



# MACHAKOS UNIVERSITY COLLEGE

(A Constituent College of Kenyatta University)  
University Examinations for 2015/2016 Academic Year

SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF PHYSICAL SCIENCES

FIRST SEMESTER EXAMINATION FOR THE DEGREE OF BACHELOR OF  
EDUCATION (SCIENCE)

SPH 300: WAVE THEORY

DATE: 3/8/2016

TIME: 11:00 – 1:00 PM

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## INSTRUCTIONS:

Answer question **ONE** which is compulsory and any other **TWO**

## SECTION A

### QUESTION ONE (COMPULSORY)

- a) i) State two characteristics of the forces responsible for simple harmonic motion. (2 marks)
- ii) Show that  $y = A\cos kx + B\sin kx$  is a solution to simple harmonic motion where  $A$  and  $B$  are constants. (3 marks)
- iii) Show that the solution in (a) (ii) can also be written in: - (3 marks)
- (I) Polar form (3 marks)
- (II) Exponential form (3 marks)
- b) For a compound pendulum,
- i) Show that it executes simple harmonic motion (4 marks)
- ii) Find equations for its periodic time and frequency (2 marks)

- c) In terms of harmonics, explain why a loaded bus is more comfortable than an empty one (3 marks)
- d) Show that energy in a purely reactive circuit is sinusoidal (4 marks)
- e) i) A 200g mass hanging from a spring causes an extension of 4 cm. If the mass was displaced and allowed to vibrate freely, calculate the period and frequency of the vibration. (4 marks)
- ii) If two springs, similar to that in (e) (i) were used in series, explain the effect on the period and frequency of the system (2 marks)

### QUESTION TWO

- a) Distinguish damped and forced vibrations (2 marks)
- b) Show that  $D = \frac{A}{\sqrt{(\omega_0^2 - \omega^2)^2 + 4\omega^2 \beta^2}}$  is the amplitude of a forced vibration for a mechanical systems of mass  $m$  and stiffness constant  $k$  where  $\omega_0 = \sqrt{\frac{m}{k}}$  and  $\omega$  is the frequency of the driving force and  $\beta = \frac{b}{2m}$  for damping constant  $b$ . (9 marks)
- c) Show that current in a R-L-C series circuit connected to a battery of emf  $\epsilon_0$  is given by  $I = I_0 e^{-i(\omega t - \theta)}$  where  $Z = |Z| e^{-i\theta}$  and  $I_0 = \frac{\epsilon_0}{Z}$  (9 marks)

### QUESTION THREE

- a) Derive the partial differential equation  $y(x,t)$ , the equation of a travelling wave. (7 marks)
- b) Show that a transverse wave in a vibrating string obeys the wave equation and hence give the velocity of the waves (7 marks)
- c) Show that a longitudinal wave in a rod of density  $\rho$  and Young's modulus  $E$  obeys the wave equation with the wave moving at  $\sqrt{\frac{E}{\rho}}$  (6 marks)

#### QUESTION FOUR

- a) i) What is meant by a coupled oscillator? Give an example of a practical system that consists of a coupled oscillator explaining the coupling involved (3 marks)
- ii) Describe the motion of a coupled system of masses in which mass  $m_1$  is displaced a distance  $A$  to the right while mass  $m_2$  is displaced an equal distance to the left. (5 marks)
- b) An alternating current through a rectifier is given as  $I = \begin{cases} I_0 \sin \theta & \text{for } 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$  where  $I_0$  is the maximum current and  $2\pi$  is the period. Express  $I$  in Fourier Series (12 marks)

#### QUESTION FIVE

- a) Show that a charged capacitor discharging through an inductor and resistor represents damped harmonic motion (6 marks)
- b) Derive an expression for the distance  $X_n$  on the screen for the  $n^{\text{th}}$  maxima in a diffraction pattern in terms of the distance from the source to the barrier,  $a$  and the distance from barrier to the screen,  $p$  (8 marks)
- c) (i) Derive an expression for the wavelength of light  $\lambda$  using the 2<sup>nd</sup> and 4<sup>th</sup> minima in a diffraction pattern. (4 marks)
- (ii) A diffracting edge is placed between a monochromatic point source of light and a screen. Given that its distance from the source is 20 cm while that from the screen is 150 cm, determine the wavelength of light used if the separation of the 2<sup>nd</sup> and 4<sup>th</sup> minima is 0.0227 cm. (4 marks)