# MACHAKOS UNIVERSITY 

University Examinations 2019/2020 Academic Year
SCHOOL OF PURE AND APPLIED SCIENCES
DEPARTMENT OF MATHEMATICS AND STATISTICS

## ...........YEAR ...... SEMESTER SPECIAL /SUPPLEMENTARY EXAMINATION FOR BACHELOR OF ENVIRONMENT STUDIES ESU 302: STATISTICS

DATE:
TIME:

INSTRUCTION: Answer Question ONE which is compulsory and any other TWO Questions

## QUESTION ONE (30 MARKS)

a) Differentiate the following terms as they apply in scientific research
i. Sample and a population
ii. Response and independent variables
iii. Descriptive and inferential statistics
iv. Null hypothesis and Alternative hypothesis
v. Type I and Type II error
b) In a class sample of 12 students, the instructor wanted to establish whether gender influenced their performance. Given below are their test scores per gender, at $\alpha=5 \%$

| Males | 8 | 12 | 13 | 9 | 3 | - | - |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Females | 10 | 8 | 12 | 15 | 6 | 8 | 11 |

i. Determine whether gender influence the class performance significantly
ii. Test the hypothesis that the mean score for females is 11.9
c) i Determine the regression equation of Y on X given that
$\sum x y=130, \quad \sum x^{2}=2400, \bar{x}=60$ and $\bar{y}=4$.
ii Highlight three assumptions for regression modeling

## QUESTION TWO (20 MARKS)

a) The data below is a summary of the slim possible participants weights in kilograms before and after the season.

| Participant | A | B | C | D | E | F | G | H |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Weight Before | 85 | 124 | 172 | 123 | 111 | 139 | 99 | 77 |
| Weight after | 105 | 160 | 175 | 143 | 156 | 127 | 95 | 100 |

Test the hypothesis that on average the exercise did not result to any significant weight loss at $10 \%$ significance level
b) Below was the daily harvest of a tropical plant during a particular week in the year 2017.

| Harvested fruits | $11-20$ | $21-30$ | $31-40$ | $41-50$ | $51-60$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 3 | 6 | 11 | 3 | 2 |

Determine;
i. Average harvest per day
ii. Median
iii. Mode and
iv. Standard deviation.

## QUESTION THREE (20 MARKS)

a) The information relates health records from County XYZ randomly selected

| Gender | Males | Females |
| :--- | :--- | :--- |
| Average lifespan | 50 | 58 |
| Standard deviation | 12 | 9 |
| Sample size | 100 | 150 |

Determine;
i. The gender with the higher dispersion lifespan
ii. The combined standard deviation
iii. State the hypotheses for testing life expectancy for the two genders
iv. Do the life span differ significantly for the two gender (use $\alpha$-level $=1 \%$ ).
(12 marks)
b) Using the data below determine if there was any correlation between the sodium concentration and Opuntia area coverage.
(8 marks)

| Sodium conc. | 1.75 | 5.83 | 5.33 | 4.67 | 7.17 | 5.50 | 9.33 | 6.83 | 7.50 | 10.80 | 11.30 | 11.40 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Opuntia area | 14.2 | 30.1 | 71.2 | 77.5 | 75.9 | 121.8 | 132.1 | 159.0 | 181.9 | 184.3 | 194.6 | 219.1 |

QUESTION FOUR (20 MARKS)
a) Differentiate between a discrete random variable and a continuous random variable
(4 marks)
b) Suppose a fair coin is tossed twice and by letting $X$ represent the number of Heads that show up. Determine $E(X)$ and $\operatorname{Var}(X)$
c) The table below shows the scores of eight interviewees on aptitude and subject matter knowledge

| Interviewee | A | B | C | D | E | F | G | H |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Aptitude test score | 15 | 20 | 28 | 12 | 40 | 60 | 20 | 80 |
| Subject matter score | 40 | 30 | 50 | 30 | 20 | 10 | 30 | 60 |

Compute the rank coefficient of correlation

## QUESTION FIVE (20 MARKS)

a) Highlight three principles of experimental design
b) By citing examples distinguish between discrete and numeric variables
c) A manufacturer wished to compare the performance of different machine brands, their performance difference is summarized in ANOVA table below.

| Source of <br> Variation | Degrees of <br> Freedom | Sum of <br> Squares | Mean sum of <br> Squares | F - value |
| :--- | :--- | :--- | :--- | :--- |
| Between <br> machines | $4-1=3$ | 540.69 | 180.23 | $F=\frac{180.23}{7.15}=25.207$ |
| Error | $16-4=12$ | 85.75 | 7.15 |  |
| Total | $16-1=15$ | 626.44 |  |  |

$\begin{array}{lll}\text { i. } & \text { Based on the table above state the number of machine brands compared } & (1 \mathrm{mark}) \\ \text { ii. } & \text { Explain the two sources of variation in column one of the table } & (2 \mathrm{marks}) \\ \text { iii. } & \text { When is it appropriate to use ANOVA and F-test for data analysis } & (4 \mathrm{marks}) \\ \text { iv. } & \text { Was there a significant difference in their performance at } \alpha=5 \% & (4 \text { marks })\end{array}$

