

# **MACHAKOS UNIVERSITY**

# University Examinations 2019/2020 SCHOOL OF PURE AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE SECOND YEAR SECOND SEMESTER EXAMINATION FOR DIPLOMA IN FOOD AND BEVERAGE

## MATHEMATICS

DATE: 29/10/2020

#### TIME: 11:30 – 2:30 AM

### **INSTRUCTIONS: Answer Question One and Any Other Two Questions**

1.	a)	A line	passes through the points $A(7,g)$ and $B(4,5)$ and is perpendicular to	) and B(4,5) and is perpendicular to the line		
		Whose	e equations 4y=3x-9. Find the value of g.	(5 marks)		
	b)	A plot	of a land is valued at sh.1, 250,000.due to increase in demand; it a	increase in demand; it appreciates		
		at the	rate of 6% every six months. What its value be after $3^{1}/_{2}$ years	(5 marks)		
	c)	the $4^{th}$ and $7^{th}$ term of a geometric sequence are 24 and 192 . Find the common ratio				
		and the	e first term of the sequence.	(5 marks)		
	d)	The su	am of the first four terms of an AP is 32 and the sum of the first sev	st four terms of an AP is 32 and the sum of the first seven terms is		
		98. Fir	nd the first term and the common difference	(5 marks)		
	e)	a line I	L passes through points (-2,3) and (-1,6) and is perpendicular to a l	ndicular to a line passing		
		through the point P at $(-1,6)$ .				
		i.	Find the equation of l in terms Y=mx+c	(2 marks)		
		ii.	Find the equation of P in form of ax+by=c where a,b,c are constant	nts.		
	f)					
		i.	7 <i>c</i> <sub>3</sub>	(2 marks)		
		ii.	5 <i>p</i> <sub>2</sub>	(2 marks)		

2.	A packet contains 3 red, 9 blue and 15 grey corks all identical in shape and size. Find the						
	prob	ability	of picking.				
	a)	i	A red cork	(1 mark)			
		ii	A non –red cork	(2 marks)			
	b)	Two corks are picked at random, one at a time without replacement. Find the					
		prob	probability that;				
		i.	A red and grey cork are picked	(3 marks)			
		ii.	Both corks are of the same colour	(4 marks)			
	c)	Two dice are tossed together once. Prepare a table to illustrate the possible spaces					
		for this experiment. Find the probability that the sum of the faces					
		i.	P (x≥6)	(3 marks)			
		ii.	P(x<8)	(2 marks)			
		iii.	P (6≤x≤12)	(3 marks)			
3.	a)	The first term of an AP is 2. The sum of the first 8 terms is 156.					
		i.	Find the common difference of the AP	(2 marks)			
		ii.	Given that the sum of the first n terms of the AP is 416, find n	(3 marks)			
	b)	The third, fifth and eighth terms of another AP forms the first three terms of a G.P. if					
		the common difference of the A.P is 3 find.					
		i.	The first of the G.P	(3 marks)			
		ii.	The sum of the first 10 terms of the G.P to 4 significant figures	(3 marks)			
	c)	Two concentric circles are radii 3.5 cm and 14 respectively. Find in terms of $=$ cm <sup>2</sup>					
		i.	The area of the inner circle	(2 marks)			
		ii.	The area of the outer circle	(2 marks)			
		iii.	The probability that a point chosen at random in the bigger circle	lies within			
			the smaller circle	(3 marks)			
		iv.	The probability that appoint chosen at random lies outside the sn	naller circle			
				(3 marks)			
4.	A pa	A paint dealer mixes three types of paint A,B and C in the ratio's A:B 3:4 and B:C1:2. The					
	mixt	mixture is to contain 168 litres of C.					
	a)	Find	the ratio A: B: C	(2 marks)			

b) Find the required number of litres of B (2 marks)

- c) The cost per litre of type A is ksh.160, type B is 205 and type C is ksh.100.
  - i. Calculate the cost per litre of the mixture (4 marks)
  - ii. Find the percentage profit if the selling price of the mixture is ksh.182 per litre (3 marks)
  - iii. Find the selling price of a litre of the mixture if the dealer makes a 25% profit (3 marks)
- d) Tap A can fill a tank in 5 hours while B can fill the same tank in 7 hours. Tap C can empty the same tank in 6 hours, how long would it take;
  - i. Tap A and B to fill the tank when its empty and tap C is closed (3 marks)
  - ii. Tap A and B to fill the empty tank with Tap C open (3 marks)