# MACHAKOS UNIVERSITY 

University Examinations 2019/2020

## SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE
SECOND YEAR SECOND SEMESTER EXAMINATION FOR
DIPLOMA IN BUILDING AND CIVIL ENGINEERING

## MATHEMATICS

DATE: 29/10/2020
TIME: 11:30-2:30 PM

## INSTRUCTIONS: Answer Question One and Any Other Two Questions

1. a) The arch length of a circle with radius 14 cm is 11 cm . find the angle subtended at the Centre of the arc.
b) A figure $A B C D$ is a trapezium in which $A D$ is parallel to $B C$. Given that $A D=25 \mathrm{~cm}$, $\mathrm{BC}=15 \mathrm{~cm}$ and angle $\mathrm{DAB}=60^{0}$, calculate the area of the trapezium. (4 marks)

c) The first term of an AP is -3 and the last term is 41 . The sum of the term is 228 . Calculate the number of terms in the AP and the common difference.
d) The third term of a G.P is 12 and the fifth term is 48 . Find the sum of the first 8 terms of the G.P given that the G.P is increasing
e) Using substitution method solves the following simultaneous equation:
$2 \mathrm{~m}-5 \mathrm{n}=1$
$3 \mathrm{~m}+4 \mathrm{n}=13$
f) Without using mathematical tables or calculator, evaluate

$$
\frac{\operatorname{Tan} 30^{\circ} \cdot \tan 60^{\circ}}{\operatorname{Sin} 60^{\circ} \cdot \cos 30^{\circ}}
$$

g) The figure below represents a plot of land $A B C D$ such that $A B=85 \mathrm{M}, \mathrm{BC}=75 \mathrm{M}$, $C D=60 \mathrm{M}, D A=50 \mathrm{M}$ and angle $\mathrm{ACB}=90^{\circ}$


Determine the area of the plot in hectares correct to 2 decimal places
2.
a)
solve the equation :

$$
\operatorname{Cos}^{2} \varnothing+\sin \varnothing+1=0
$$

b) Calculate the length AD in the figure below given that $\mathrm{BC}=3.63 \mathrm{CM}$, $A C=2.76 \mathrm{~cm}$, angle $B=41.8^{\circ}$ and angle $D=30^{\circ}$

c) Use the data below to evaluate

2, 4,6,8,11,13.
i. Mean
ii. Median
iii. Mode
d) Solve the equation
$7 \mathrm{p}-2=-2 \mathrm{p}^{2}$
3. a) complete the table below for the function
$\mathrm{Y}=\mathrm{X}^{2}-6 \mathrm{X}+7$

| X | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| X 2 |  |  |  |  |  |  |
| -6 X |  |  |  |  |  |  |
| +7 |  |  |  |  |  |  |
| $\mathrm{Y}=\mathrm{X}^{2}-6 \mathrm{X}+7$ |  |  |  |  |  |  |

b) On the grid provided draw the graph of $Y=X^{2}-6 X+7$ (booklets with grids required)

For $0 \leq \mathrm{X} \leq 6$ and use it to estimate the roots to the equation
(8 marks)
$x^{2}-6 x+7=0$
c) Use the graph above to solve the equation

$$
x^{2}-7 x+9=0
$$

d) Solve the equation $(a+1)^{2}+3 a-1=0$ (5 marks)
4. a) The third, fourth and fifth terms of a G.P are $t+4, t+10$ and $t+20$ respectively.

Determine the
i. Common ratio
ii. First term
iii. Sum of the first 12 terms
b) The firth and eleventh terms of an arithmetic progression are 27 and 45 respectively.

Determine the;
i. $\quad 30^{\text {th }}$ term
ii. Sum of the first 16 terms

