## MACHAKOS UNIVERSITY

## UNIVERSITY EXAMINATION 2020/2021 <br> SCHOOL OF PURE AND APPLIED SCIENCES <br> DEPARTMENT OF MATHEMATICS,STATISTICS AND ACTUARIAL SCIENCE <br> SECOND SEMESTER FIRST YEAR FOR <br> 1920/104- CRAFT CERTIFICATE IN INFORMATION COMMUNICATION TECHNOLOGY 1920/104- MATHEMATICS

1.explain the following as applied in probability
i) mutually exclusive events
ii) random variables
2.convert each of the following number systems to their respective equivalents, showing your working.
i) $475_{8}$ to binary
ii) $7 B 2 D_{16}$ to denary
3.with the aid of examples in each case distinguish between lower triangular matrix and identity matrix
4.using the graphical method, solve the quadratic equation $y=2 x^{2}-12 x+16$,for $0 \leq x \leq 5$.

5 i) using binomial theorem, expand the expression $(2+x)^{4}$ in ascending powers of $x$, simplifying the results
ii) using Pascal's triangle ,determine the coefficients of the expression $(a+b)^{4}$

6 a) determine the equation of the line passing through point $(18,6)$ and has a gradient of -12 ( 2 mks )
b) the size of matrix $X$ is a 5 by 3 matrix and the product of $X Y$ is a matrix of size 5 by 7 matrix.

Determine the size of matrix Y .
(3mks)
7. a) the ages of 6 students in a class are:

17,15,18,21,14,19
Determine the median age
b) given the following matrix:
determine the value of $B^{-1}$
8 (a) the probability that Tom and Mary will pass in an interview is 0.4 and 0.5 respectively.
(b)solve the following inequality

$$
(5 x+5) /-10 \leq 2 x-1
$$

9 a) in a class of 100 students , 45 study history, 53 study English and 15 study both subjects. Using Venn diagram determine the number of students who study neither English nor history.
10.outline two advantages of range as measure of dispersion

Given the matrix
$A=$
Determine $\left(A^{\top}\right)^{-1}$
11. a) in a particular cyber café, the probability of one of the computers to fail to operate is 0.15 . if 5 computers are selected at random, using tree diagram determine the probabilities that:
i) 2 computers will fail to operate
ii) less than 3 computers will fail to operate
iii)4 computers will operate
iv)at least 1 of the computers will fail to operate
b) explain the meaning of the following as used in set theory:
i)universal set
ii)subset
iii)empty set
12. a) the following is a distribution table of profits of companies in the same industry

| Profit(ksh 000's) | Number of companies |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | 15 |
| $20-30$ | 40 |
| $30-40$ | 20 |
| $40-50$ | 16 |
| $50-60$ | 4 |

## Calculate the:

i) Mean
ii) Median
iii) Standard deviation
iv) Pearson's coefficient of skewness
b) explain three properties of a normal distribution curve
13.solve the following simultaneous equations using matrix method

$$
\begin{align*}
& 8 x+12 y+4 z=368 \\
& 4 x+10 y+4 z=264 \\
& 10 x+4 y-2 z=216 \tag{6mks}
\end{align*}
$$

b) a survey of 210 jobs applicants was carried out to determine whether they were competent in three languages: French, Spanish and Japanese. The following were the results:

10 were competent in all the three languages
18 were competent in both Japanese and French
22 were competent in Japanese and Spanish
48 were competent in Spanish and French
104 were competent in French
126 were competent in Spanish
50 were competent in Japanese
i) Present the information above in a venn diagram
ii) Determine the number of applicants that were competent in:
(a)Spanish but not French
(b)Japanese but not French
(c)neither Spanish not French
(d)Spanish or French
(e)both French and Spanish but not Japanese
14.(a) A shop sold three types of products; $A, B$ and $C$ on a cetain day as follows:

2 units of $A, 3$ units of $B$ and 1 unit of $C$ for ksh 490 .
3 units of $A, 4$ units of $B$ and 2 units of $C$ for ksh 700
1 unit of $A, 2$ units of $B$ and 1 unit of $C$ for ksh 330
(i) Formulate simultaneous equations to represent the information above
(ii) Using elimination method determine
(a) Price per unit of each of the three products;
(b) Total amount to be paid for 4 units of $A$ and 2 units of $B$
(b)explain three challenges that an organization may encounter from the use of computers in its operations
15.(a)using relevant examples define the following as applied in matrix
(a)diagonal matrix
(b)singular matrix
(c)identity matrix
(d)null matrix
(e)singular matrix
(f)unit matrix
b)a group of 6 boys has a mean weight of 54 kg .when 2 more boys joined the group, one with $x$ kg and the other with $(x+10) \mathrm{kg}$, the new mean is 55 kg . determine the value of $x$
c) a committee of three people is to be selected from a group of eight people. Determine the number of possible ways of forming the committee.

