MACHAKOS UNIVERSITY
University Examinations 2019/2020 Academic Year
SCHOOL OF PURE AND APPLIED SCIENCES
DEPARTMENT OF MATHEMATICS AND STATISTICS
FOURTH YEAR SPECIAL /SUPPLEMENTARY EXAMINATION FOR

## BACHELOR OF SCIENCE IN MATHEMATICS AND COMPUTER SCIENCE

BACHELOR OF SCIENCE IN STATISTICS AND PROGRAMMING
BACHELOR OF SCIENCE IN MATHEMATICS
SMA 467: TEST OF HYPOTHESIS II
DATE: 21/1/2021
TIME: 2.00-4.00 PM

## INSTRUCTIONS

1. Answer Question $\mathbf{1}$ and any other two questions.
2. Out of the three questions answered, each question must start on a new page.
3. You need the following items for this paper:

- Scientific Calculator.
- Statistical Tables.


## QUESTION ONE (30 MARKS)

a) (i) Define the term test of hypothesis as used in Statistics.
(ii) Differentiate between a one-tailed test and a two-tailed test as used in statistical test of hypothesis.
b) The following is a set of marks scored in Mathematics in an examination by a class comprising of 24 students from a certain high school.

| 50 | 44 | 25 | 28 | 32 | 58 | 42 | 81 | 66 | 20 | 18 | 35 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 28 | 68 | 46 | 72 | 24 | 37 | 32 | 36 | 48 | 45 | 86 | 64 |

Test the set of marks for randomness at the $5 \%$ level of significance. Note: median $=43$.
(6 marks)
c) The following data set represents the marks scored by a random sample of 14 male students and 12 female students who sat for end of semester paper in general statistics.

| Male | 58 | 68 | 32 | 64 | 54 | 44 | 56 | 62 | 66 | 60 | 52 | 55 | 75 | 61 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Female | 45 | 72 | 48 | 55 | 65 | 35 | 70 | 55 | 53 | 74 | 73 | 67 |  |  |

Using the Mann-Whitney $U$ test, assess whether there is a statistically significant difference in the academic performance between the male and female students. Take level of significance $\alpha=5 \%$.
d) A educational researcher carried out a study on the relationship between the student academic performance in Statistics and the degree course programme taken by the students. A random sample of 500 students was selected, and the data pertaining to the academic performance and the course programme summarised in the contingency table below.

|  | Mathematics | Economics | Agriculture |
| :--- | :--- | :--- | :--- |
| Distinction | 96 | 26 | 10 |
| Credit | 120 | 70 | 24 |
| Pass | 84 | 54 | 16 |

Test whether there is a relationship between the student academic performance and the degree programme taken by the students. Use the $5 \%$ and the $1 \%$ levels of significance.
(10 marks)

## QUESTION TWO (20 MARKS)

a) State two advantages and two disadvantages of non-parametric tests of hypothesis. (4 marks)
b) Explain any two circumstances in which the Spearman's rank correlation co-efficient is suitable in the analysis of statistical data.
c) A study was carried out to determine whether there is a difference in salaries between men and women among married couples. A random sample of 15 couples was selected in a certain town and the monthly salaries in thousand Kenya shillings were as shown in the table below.

| Couple | A | B | F | P | E | F | H |  | K | L | M | N | P | Q |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Male | 72 | 42 | 66 | 64 | 25 | 18 | 70 | 65 | 82 | 28 | 45 | 34 | 52 | 41 | 75 |
| Female | 36 | 40 | 35 | 48 | 34 | 24 | 32 | 22 | 37 | 30 | 52 | 24 | 44 | 43 | 40 |

Using the Wilcoxon signed rank test for paired data, evaluate whether the two sets of salaries are the same. Use the $5 \%$ level of significance.

## QUESTION THREE (20 MARKS)

An engineering company has developed two types of devices for estimating long distances between two points on the earth surface. One device uses terrestrial communication while the other uses satellite communication. In evaluating them, 12 random distances were taken between various points and the actual distance and also the distance estimated by each of the two devices recorded in kilometres as shown in the table below:

| Distance | A | B | C | D | E | F | G | H | J | K | L | M |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Actual | 15 | 19 | 18 | 30 | 62 | 30 | 78 | 23 | 68 | 55 | 30 | 17 |
| Terrestrial | 24 | 26 | 48 | 64 | 40 | 54 | 45 | 48 | 72 | 32 | 48 | 25 |
| Satellite | 20 | 25 | 28 | 23 | 48 | 64 | 82 | 28 | 90 | 65 | 45 | 10 |

a) (i) Compute the Spearman's rank correlation co-efficient between the actual distance and the estimated distance by terrestrial device, and between the actual distance and the estimated distance by satellite based device.
(ii) Interpret each of the co-efficients of correlation obtained in (i) above.
b) Recommend the most suitable device for estimating distance, justifying your choice based on the results obtained in (a) above.
c) Test for significance each of the two co-efficients of correlation obtained in (a)(i) above.

## QUESTION FOUR (20 MARKS)

a) An educational researcher claims that the pass rates for subjects in KCSE vary with the proportion of students who pass in some of the subjects is as shown below:

| English | $60 \%$ | History | $70 \%$ |
| :--- | :--- | :--- | :--- |
| Mathematics | $35 \%$ | Physics | $20 \%$ |
| Kiswahili | $50 \%$ | Biology | $60 \%$ |
| Geography | $75 \%$ |  |  |

A random sample of $\mathbf{5 0 0}$ KCSE candidates in a certain year was taken for students who sat for all the seven listed subjects, and the number of candidates who passed in the seven subjects is as shown below:

| English | 240 | History | 420 |
| :--- | :--- | :--- | :--- |
| Mathematics | 105 | Physics | 125 |
| Kiswahili | 210 | Biology | 330 |
| Geography | 420 |  |  |

Using chi-square test for goodness of fit, evaluate whether this claim about KCSE pass rates is true or not at the $5 \%$ level of significance.
b) A manufacturer claims that only $1 \%$ of the items from the production line are faulty or defective. The items are produced in batches of 300 items per batch.
A quality control official took a random sample of 250 batches and tested all the items in each batch and found out the following on the number of defectives items per batch.

| Defective items $(x)$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No of batches $(f)$ | 10 | 28 | 44 | 48 | 45 | 35 | 24 | 10 | 4 | 2 |

Using the chi-square test for goodness of fit, evaluate whether this claim by the manufacturer is true or not at the $5 \%$ level of significance.
(12 marks)

## QUESTION FOUR (20 MARKS)

a) In a certain mango farm, there are different varieties of mangoes planted randomly and grown under similar conditions. The number of fruits in thousands from three random samples of mango trees in the farm is as shown in the table below.

| Sample 1 | 3.8 | 3.0 | 4.2 | 2.5 | 2.6 | 3.2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample 2 | 2.9 | 2.7 | 3.3 | 4.0 | 2.4 |  |
| Sample 3 | 2.8 | 3.4 | 3.6 | 3.7 | 2.2 | 3.5 |

Using the Kruskal-Wallis test, evaluate whether the three samples of mangoes are drawn from the same variety or not at the $5 \%$ level of significance.
(8 marks)
b) Given a set of $n$ bi-variate observations comprising pairs of variables $\left(x_{i}, y_{i}\right)$, derive the formula for the Spearman's rank co-efficient of correlation given by:

$$
\begin{equation*}
r_{x y}=1-\frac{6 \sum\left(R_{x}-R_{y}\right)^{2}}{n\left(n^{2}-1\right)} \tag{12marks}
\end{equation*}
$$

