



**MACHAKOS UNIVERSITY**  
**ISO 9001:2008 Certified** 

**UNIVERSITY EXAMINATIONS 2020/2021**

**UNIVERSITY SUPPLEMENTARY EXAMINATIONS  
FOR THE DEGREE OF BACHELOR OF SCIENCE COMPUTER SCIENCE**

**CSO 108: DISCRETE MATHEMATICS**

**INSTRUCTIONS TO CANDIDATES**

**(a) Answer ALL the questions in Section A and ANY THREE Questions in Section B**

**SECTION A**

**QUESTION ONE 30 Marks (Compulsory)**

- a) Define the following terms.
- i). A graph
  - ii). trail
  - iii). Set
  - iv). Proposition
  - v). A subset (5 marks)
- b) Find the power set of the set  $A = \{1,2,3,4\}$ . (3 marks)
- c) Construct all the unlabeled graphs with 4 vertices (5 marks)
- d) Construct the truth table for the disjunction of two proposition (4 marks)
- e) In how many distinguishable ways can the product  $Z^7 X^8 Y^7 T^6$  be arranged without using exponents. (3 marks)
- f) Given  $A = ((abc)'c)'(a' + c)(b' + ac)'$  express it as a sum of product expression. (5 marks)
- g) Prove that if a bipartite graph has a cycle then all its cycles are of even length. (5 marks)

**QUESTION TWO 20 MARKS**

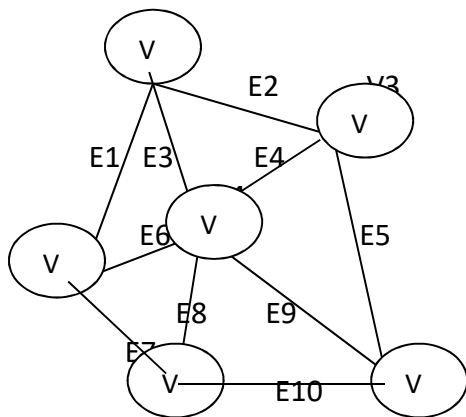
- a) Construct the logic circuit for the following output  $Y = (XY + ZY')' + (X' + ZY)'$  (5 marks)
- b) Show that  $D_{210}$  (where  $D_{210}$  are divisors of 210) is a Boolean algebra
- Find the atoms (3 marks)
  - Find the subalgebra (3 marks)
  - Construct the lattice diagram (4 marks)
- c) Given that  $X = 00111001$   $Y = 11100011$   $Z = 00110010$   $T = 01011011$ . Find
- $$A = X.Y.Z.T + TZ \quad (5 \text{ marks})$$

### QUESTION THREE 20 MARKS

- a) Given that  $a$  and  $b$  are rational with  $b \neq 0$  and  $s$  is an irrational number such that  $a - bs = t$ . Show that  $t$  is irrational hence show that  $\frac{-1+\sqrt{3}}{1+\sqrt{3}}$  is irrational (6 marks)
- b) Show that  $\sqrt{5}$  is irrational (5 marks)
- c) Proof that set of all even natural numbers is countable. (5 marks)
- d) Suppose two boys say Fred and Sum are playing a Football tournament such that the first person to win two games in a row or who wins a total of three games wins the tournament. Construct a rooted tree to illustrate the above. Find the number of ways the tournament can be won. (5 marks)

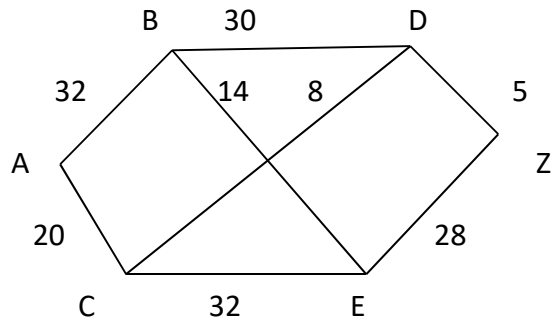
### QUESTION FOUR 20 MARKS

- a) Prove that if  $G$  is a connected planar graph with  $P$  vertices and  $q$  edges. Where  $p \geq 3$ . then  $q \leq 3p - 6$ . (5 marks)
- b) Construct the Incidency matrix for the following graph. (5 marks)



c) Find the shortest path from A to Z for the map shown below

( 5 marks)



a) Prove that if  $M$  is a map with  $V$  vertices,  $E$  edges and  $R$  regions and  $K$  components. Then

$$V - E + R = K + 1.$$

(5 marks)

**QUESTION FIVE 20 MARKS**

a) Let  $U = \{i, j, k, l, m, n, o, p, q, r, s, t, u\}$ ,  $A = \{i, k, l, m, q\}$   $B = \{j, k, q, r\}$   
 $C = \{j, k, m, o\}$  and  $D = \{j, o, p\}$ .

Determine the set

i)  $A \cup B$

ii)  $A \cap C$

iii)  $(A \cup B) \cap C^c$

iv)  $(C \cap A) \cup D$

v)

( 8 marks)

b) Let  $A = \{s, t\}$  and  $B = \{1,4,6\}$  determine the set

$(A \times B) \times B$  (2marks)

c) A man who works five days a week can travel to work on foot, by bicycle or by bus. In how many ways can he arrange a week's travelling to work? (6 marks)

d) Show that  $[p \vee q]$  and  $p \rightarrow q$  are logically equivalent

(6 marks)

