

# MACHAKOS UNIVERSITY

University Examinations 2020/2021 Academic Year SCHOOL OF PURE AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS AND STATISTICS FIRST YEAR FIRST TERM EXAMINATION FOR CERTIFICATE IN ELECTRICAL ENGINEERING

**AUTOMOTIVE ENGINEERING** 

1601/103: ELECTRICAL MATHEMATICS I

1503/103: AUTOMOTIVE MATHEMATICS 1

DATE: 3/6/2021 TIME: 11.30-2.30 PM

### **INSTRUCTIONS:**

Answer ALL the Questions

Show ALL your working clearly

#### **QUESTION ONE**

- a) Simplify the following:
  - i.  $69 \div \{6 + (3 \times 8 7)\}$
  - ii.  $2\frac{1}{2} \times 1\frac{1}{3} \frac{3}{5} \div 1 + \frac{4}{11}$
  - iii.  $\frac{2a-4b}{4} \frac{a-b}{3}$  (11 marks)
- b) Determine the length of the shortest piece of a string that can be cut into equal lengths, each 42cm, or 35cm, or 28cm (5 marks)
- Given that John has 60 books and  $\frac{1}{3}$  of Josephs's books are the same as  $\frac{3}{4}$  of John. How many books has Joseph? (4 marks)

#### **QUESTION TWO**

- a) i Express in logarithmic notation  $a = b^c$ 
  - ii Express in index notation  $log_a x = -3$
  - iii Express as a single logarithm  $3\log 2 2\log 6 + 2\log 3$  (5 marks)

b) Simplify (i) 
$$\frac{(2^3)^4 x (3^2)^2}{16^2 x 9^3}$$
 using indices

(ii) 
$$\log 25 - \log 625 + \log 125$$
 (6 marks)

c) Solve the following equations

i. 
$$\frac{a^3 x a^x}{a^2} = a^8$$

ii. 
$$1 - \log(x - 6) = \log x$$

iii. 
$$\left(\frac{1}{4}\right)^y = (32)^{3-y}$$
 (9 marks)

#### **QUESTION THREE**

a) Use logarithms to evaluate

$$\sqrt{\frac{0.0782 \times 34.39}{4.836}}$$
 (7 marks)

b) Evaluate

i. 
$$log_3 \frac{1}{81}$$

ii. 
$$\frac{18^0 \times 16^{\frac{1}{2}}}{8}$$
 (6 marks)

c) Solve the following equation

$$3^{x+1} = 2^{2x-3}$$
 correct to 2 d.p (4 marks)

d) State the number of significant figures in the following measures

i. 6010 km

ii. 42.058 hrs

iii. 
$$85000 \text{cm}^3$$
 (3 marks)

#### **QUESTION FOUR**

a) Evaluate

i. 
$$\frac{8 \times 10^{11} \times (2 \times 10^{-3})^4}{3.2 \times 1.6 \times 10^8}$$
 giving your answer in standard form

ii. 
$$(-3)^2 x (-3)^3 \div (-3)^4$$

iii. 
$$\left(\frac{16}{81}\right)^{\frac{1}{4}} \times \frac{2^0 \times 3^{-2}}{5^{-1}}$$
 (10 marks)

b) Express the following in fraction form

i. 0.7

c) If  $2^a x 3^b = 72$ , what are the numerical values of a and b (4 marks)

## **QUESTION FIVE**

a) Simplify

i. 
$$\frac{12z^{12}}{4z^2 \times 3z^6}$$

ii. 
$$3^{n+1} \times 9^n \div 27^{\frac{2}{3}n}$$
 (6 marks)

b) Evaluate

i. 
$$3x^2 x 2xy + z^3$$
 when  $x = -2$ ,  $y = 2$ , and  $z = -1$ 

ii. 
$$27.19 \times 0.573$$
 and give the answer in standard form correct to 3 s.f. (5 marks)

c) Convert

i. 87 to binary

ii. 
$$11101_2$$
 to octal (5 marks)

d) Solve for x, 
$$\frac{x+1}{3} - \frac{x-2}{4} = \frac{x}{6}$$
 (4 marks)