



MACHAKOS UNIVERSITY COLLEGE

(A Constituent College of Kenyatta University)

University Examinations 2014/2015

SCHOOL OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF COMPUTING AND INFORMATION TECHNOLOGY

FIRST YEAR FIRST SEMESTER EXAMINATION FOR DEGREE IN BACHELOR OF SCIENCE IN INFORMATION TECHNOLOGY

INTRODUCTION TO LOGICS

DATE: 10/12/2014

TIME: 8:30 – 10:30 AM

QUESTION ONE (30 MARKS)

- (a) Define the following terms as applied to logics
- (i) Graphical logics (2 marks)
 - (ii) Propositions (2 marks)
 - (iii) Causal (2 marks)
 - (iv) Premise (2 marks)
- (b) (i) What is Boolean algebra? (2 marks)
(ii) Name the operators permitted in Boolean algebra. (3 marks)
- (c) Consider the following sentences
- (i) The sum of the numbers 5 and 3 equals to 8
 - (ii) May good fortune come your way
- Which of the above sentences is declarative in nature and which ? Explain why.
(8 marks)
- (d) (i) What is a truth table? (2 marks)
(ii) Name the features of a truth table. (6 marks)
(iii) What is tautology? (1 mark)

QUESTION TWO (20 MARKS)

- (a) State the following Boolean laws. (1 mark)
- (i) Commutative law (2 marks)
 - (ii) Associative law (2 marks)
 - (iii) Distributive law
- (b) Prove the following Boolean equality using a truth table (14 marks)
- $$(A+B)(A+C) = A + BC$$

QUESTION THREE (20 MARKS)

- (a) From a simple electrical circuit, deduce the truth table of the following logic gates
- (i) AND (4 marks)
 - (ii) OR (4 marks)
 - (iii) NOT (4 marks)
- (b) (i) State the rule for elimination implication. (2 marks)
- (iii) On using symbols Φ and Ψ write an equation to represent the above rule. (6 marks)

QUESTION FOUR (20 MARKS)

- (a) Consider the following sentences
- (i) P: " I won the lottery last week"
 - (ii) Q:" I purchased a lottery ticket"
 - (iii) R:" I won last week's sweepstake"
- Symbolically show that "IF p and q, the not r or q. (8 marks)
- (b) Use the rule of natural deduction to prove that $p \wedge q, r \vdash q \wedge r$ is valid (use the declarative sentences in Q.4 (a). (12 marks)

QUESTION FIVE (20 MARKS)

Use the rule of double negation to prove the following sequent

$p \neg\neg (q \wedge r) \vdash \neg\neg p \wedge r$ (Use the declarative sentences in (Q.4)