# MACHAKOS UNIVERSITY 

## University Examinations 2021/2022 Academic Year

SCHOOL OF PURE AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS AND STATISTICS FOURTH YEAR FIRST SEMESTER EXAMINATION FOR BACHELOR OF SCIENCE (STATISTICS AND PROGRAMMING) SST 401 -DECISION THEORY

DATE: 23/8/2022
TIME: 2.00-4.00 PM
INSTRUCTION:
Answer Question One and Any Other Two Questions
QUESTION ONE (30 MARKS)
a) Explain the meaning of the following terms as applied in decision theory
i. Opportunity loss
ii. Stochastic situation
iii. Roll-back technique
b) Differentiate between each of the following terms as applied in decision theory
i. Marginal profit and Marginal loss
ii. Minimax and minimin decision rule
c) Prepare a decision tree for the information given in the following decision matrix relating to cost data:

| State of nature <br> $P r$ | Fire | No fire |
| :--- | :--- | :--- |
| 0.01 | 0.99 |  |
| Alternatives |  |  |
| Insure | Ksh 1000 | Ksh 1000 |
| Do not insure | Ksh80000 | Ksh 0 |

d) A finance controller expresses indifference between a certain profit of ksh 6000 and a venture with a 80 per cent chance of making ksh 10000 and 10 per cent chance of making nothing. If the controller's utility scale was set at 0 utiles for ksh 0 and 100 for ksh 10000, workout the utility index for ksh 6000
e) Suppose a businessman wants to decide whether to stock commodity X or commodity Y.He can stock either but not both. If he stocks X and if it is a success, he feels he can make ksh 200 and if it is a failure he will loose ksh 500 . If he stocks Y and if it is a success, he feels that he can make ksh 400 and if it is a failure he will loose ksh 300. Which commodity X or Y should he stock if he has the following probability distribution in view:

| Probability of | With stock of <br> commodity $X$ | With stock of <br> commodity $Y$ |
| :--- | :--- | :--- |
| Success | 0.80 | 0.60 |
| Failure | 0.20 | 0.40 |

f) The marginal loss on Washington Reds, a brand of apples from the state of Washington is $\$ 35$ per case and the marginal profit is\$15 per case. During the past one, the mean sales of Washington Reds in cases was 45000 cases and the standard deviation was 4450.Assuming that the sales follow a normal distribution, determine how many cases of Washington Reds should be brought to the market.
(5 marks)

## QUESTION TWO (20 MARKS)

a) Rick Miller has just opened a new bakery in Frisco, Colorado, called morning Fresh. In performing an economic analysis, Rick has determined that the marginal cost or loss for each dozen doughnuts sold is $\$ 4$.The marginal profit is estimated to be $\$ 2.75$ per dozen doughnuts. At this time Rick is considering stocking $10,15,20,25$, or 30 dozen doughnuts. The probability of selling 10dozen doughnuts is $10 \%$, 15 dozen doughnuts is $20 \%$, and $30 \%$ chance that the bakery can sell either 20 or 25 dozen doughnuts. There is also $10 \%$ chance of selling 30 dozen doughnuts, which is considered by Rick to be the most that Morning Fresh would accommodate. Use marginal analysis to advise Rick.
(8 marks)
b) A company has three different security systems models namely: standard, deluxe, and super. An analysis of the probable acceptance of the models has been carried out and the pay -off table is shown below;

| Model acceptance | Acceptance <br> probability | Profit sh'000' (Model type) <br> Standard |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Deluxe |  |  |  |  |$\quad$ Super $\quad$.

i. Decide which model should be introduced to the market using:

- Expected pay off rule
- Minimin decision rule.
(4 marks)
ii. In the context of this question outline briefly the limitations of the two decision criteria used.
(2 marks)
iii. What would be the value of knowing the model acceptance level before making the decision on which model to produce?


## QUESTION THREE (20 MARKS)

a) Consider the following pay-off matrix table

|  | Act |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Event | Probability | A1 | A2 | A3 |
| DI | 0.3 | 10 | 20 | 30 |
| D2 | 0.5 | 40 | -10 | 20 |
| D3 | 0.2 | 20 | 50 | 50 |

i. Determine which act to choose using the maximum expected pay-off (4 marks)
ii. Determine the expected pay-off under certainty (with perfect information. (4 marks)
iii. Using the answers in (i) and (ii) above calculate the expected value of perfect information.
(2 marks)
b) A businessman has to select two independent investments A and B available to him but he has the capital to undertake both of them simultaneously. He can choose to take A first and the stop, or if $A$ is successful then take $B$, or vice versa. The probability of success on $A$ is 0.7 while for B it is 0.4 .Both investments require an initial capital outlay of ksh 2000 and both return nothing if venture is unsuccessful. Successful completion of A will return ksh 3000 (over cost), successful completion of B will return ksh 5000 (over cost). Draw a decision tree and determine the best strategy.
(10 marks)

## QUESTION FOUR (20 MARKS)

a) The following payoff table provides the profits for each of four alternatives in each of the three states of nature;

| Event | Action |  |  |
| :---: | :--- | :--- | :--- |
|  | 1 |  | -2 |
| A | 4 | 6 | 3 |
| B | 0 | 9 | 2 |
| C | -5 | 1 | 4 |
| D | 3 | 2 |  |

The probabilities for the states of nature are; $P(A)=0.2, P(B)=0.4, P(C)=0.3$ and $\mathrm{P}(\mathrm{D})=0.1$
i. Develop a conditional opportunity loss table.
ii. Hence use the Expected opportunity Loss value to determine the best decision.
b) A manager expresses indifference between an investment that will yield a certain return of ksh 10000 and a risky venture with 50 per cent chance of ksh 30000 profit and a 50 per cent chance of loss of ksh 1000.The manager utility function is as follows:

| Money ksh | -1000 | 0 | 5000 | 20000 | 30000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Utility | -2 | 0 | 10 | 20 | 30 |

A new risky venture is proposed. The possible payoffs are either ksh 0 or ksh 20000
i. Determine what probability combination of ksh 0 and ksh 20000 would make the manager indifferent to the certain ksh 10000.
ii. Explain the limitations of utility functions.

## QUESTION FIVE (20 MARKS)

a) Suppose a grocer is faced with a problem of how many cases of milk to stock to meet the daily demand. All cases of milk left at the end of the day are worthless. Each case of milk is sold at ksh 80 and is purchased for ksh 50 . Hence, each case sold brings a profit of ksh 30 but if it not sold at the end of the day, then it is discarded resulting in a loss of ksh 50.The historical record of the number of cases of milk demanded is as follows:

| Number of cases of milk demanded | Number of times demanded |
| :--- | :--- |
| $0-12$ | 0 |
| 13 | 5 |
| 14 | 10 |
| 15 | 20 |
| 16 | 30 |
| 17 | 25 |
| 18 | 10 |
| Over 18 | 0 |
| Total | 100 |

Use marginal analysis to determine the optimal decision for the grocer to maximize daily demand.
b) A security company has to decide whether to develop a new type of security device. If it does go ahead, successful completion depends on a research breakthrough. There is thought to be a 60 per cent chance of achieving. If the device is successfully developed, the payoff is a profit of ksh 900000 ; if the development is attempted but not completed, there will be a loss of ksh400000.All overheads and other sunk costs should be ignored.
i. Draw a decision tree for the information
ii. Determine the expected monetary value (EMV) of the whole decision
iii. Explain whether the term "perfect information" mean that the payoff of ksh900000 would certainly be achieved
iv. Calculate the expected value of the perfect information.

