



# MACHAKOS UNIVERSITY

University Examinations for 2021/2022 Academic Year

DIRECTORATE OF TVET

FIRST YEAR SECOND TERM EXAMINATION FOR

DIPLOMA IN ELECTRICAL AND ELECTRONICS ENGINEERING (POWER OPTION)

(TELECOMMUNICATION OPTION)

MATHEMATICS 11

DATE: 22/4/2022

TIME: 8.30-11.30 AM

## INSTRUCTIONS

You should have the following for this examination:

Mathematical tables/ Non programmable scientific calculator

Answer any five questions in the answer booklet provided.

All questions carry equal marks.

1. a) Given the matrices;

$$A = \begin{bmatrix} 2 & 1 & 2 \\ 1 & -2 & 3 \end{bmatrix} \quad B = \begin{bmatrix} 1 & -1 \\ 2 & 1 \\ 3 & 2 \end{bmatrix} \quad \text{and} \quad C = \begin{bmatrix} 2 & 1 & 2 \\ 3 & -1 & -3 \\ -6 & -2 & -8 \end{bmatrix} \quad \text{determine;}$$

i.  $BA$

ii.  $N = BA + C$

iii.  $N^{-1}$

(11 marks)

b) Three currents  $I_1$ ,  $I_2$  and  $I_3$  in an electric circuit satisfy the simultaneous equations;

$$I_1 + I_2 + I_3 = 12$$

$$2I_1 - 3I_2 + 2I_3 = 4$$

$$-4I_1 + 2I_2 + I_3 = 1$$

Use Cramer's rule to determine the values of the currents. (9 marks)

2. a) Give the vectors  $\vec{A} = 2i - 3j + 4k$  and  $\vec{B} = -3i + 2j - 6k$ , determine;
- The angle between  $\vec{A}$  and  $\vec{B}$
  - A vector  $\vec{C}$  that is perpendicular to both  $\vec{A}$  and  $\vec{B}$  (9 marks)
- b) An electric potential  $V_{(x,y,z)} = 2x^2y + zy^2$  exists in a region of space. Determine at the point (1,1,-2)
- Grad  $V$
  - Div(Grad  $V$ )
  - The directional derivative of  $V$  in the direction of the vector  $\vec{A} = 2i + 3j + k$  (11 marks)

3. a) A continuous random variable  $X$  has a probability density function defined by;

$$f(x) = \begin{cases} c(1-x)^2 & , 1 < x < 4 \\ 0 & , elsewhere \end{cases} \text{ find the;}$$

- Value of the constant  $c$
  - Mean
  - $p(1.5 \leq x \leq 2.5)$  (8 marks)
- b) The lifespan of electric bulbs are normally distributed with a mean life of 2000 hrs. and a Standard deviation of 120 hrs. Determine the probability that the life span of a bulb will be;
- Greater than 2150 hours
  - Less than 1910 hours
  - Between 1850 and 2090 hours (12 marks)

4. a) The relationship between the voltage  $V$  and the current  $I$  in an electric circuit is as shown in table 1

I	0	1	2	3	4	5
V	0.5	2.5	6.5	8.5	12.5	14.5

Determine the regression equation line of  $V$  and  $I$  (10 marks)

b) Table 1 below shows the marks scored by students in a mathematics examination

Marks	12-14	15-17	18-20	21-23	24-26	27-29
No of students	2	6	a	8	4	1

Given that the mean is 19.9, determine the;

- i. value of a
  - ii. standard deviation (10 marks)
5. a) Find  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$  given that  $z = \frac{x-y}{x^3+y^2}$  (4 marks)
- b) Use partial differentiation to determine the equation of the tangent to the curve  $z = x^2 + 3xy + y^2 - 2x - 2y$  at the point (1,1) (7 marks)
- c) Locate the stationary points of the function  $z = 2x^2 + 3y^2 - xy - 3x + 7y$  and determine their nature (9 marks)
6. a) A machine produces 11% defective resistors. Determine the probability that in a sample of 8 resistors chosen at random:
- i. exactly 3 are defective
  - ii. atleast two are defective (5 marks)
- b) Given the vectors  $\vec{A} = i + 2j + 3k$ ,  $\vec{B} = -i + 2j + k$  and  $\vec{C} = 4i + 4j$  determine  $x$  such that  $\vec{A} + x\vec{B}$  is perpendicular to  $\vec{C}$  (5 marks)
- c) Given the matrices  $A = \begin{bmatrix} 2 & 4 & -6 \\ 4 & 0 & 2 \\ 6 & 2 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 4 & -4 & 6 \\ 2 & -2 & 4 \\ 4 & 2 & 2 \end{bmatrix}$
- i. Find  $3A - 4B$
  - ii. Show that  $(AB)^T = B^T A^T$  (10 marks)
7. a) Show that the general solution of the differential equation;  $x^2 \frac{dx}{dy} = 2xy + y^2$  may be expressed in the form  $x(x+y) = cy$  where  $c$  is an arbitrary constant (9 marks)
- b) Using the method of undetermined coefficients, solve the differential equation;

$$\frac{d^2y}{dt^2} + 4\frac{dy}{dx} + 3y = t^3 + t^2 + 2$$

(11 marks)