# MACHAKOS UNIVERSITY 

University Examinations 2016/2017

SCHOOL OF PURE AND APPLIED SCIENCES
DEPARTMENT OF MATHEMATICS AND STATISTICS
FOURTH YEAR FIRST SEMESTER EXAMINATION FOR
BACHELOR OF SCIENCE (STATISTICS AND PROGRAMMING)
BACHELOR OF SCIENCE (MATHEMATICS)
SMA 461: OPERATION RESEACH II

DATE: 28/7/2017
TIME: 8:30-10:30 AM
INSTRUCTIONS
Answer question ONE (Compulsory) and any other TWO questions

QUESTION ONE (COMPULSORY) (30 MARKS)
a) Distinguish the following terms in reference to traffic flow theorem
i. Microscopic and Macroscopic traffic flow models
ii. Space head way and time head way
b) Distinguish between the König's- Egeurary theory and the König's Hall Theory
c) Sate the Birkoff- Newman theorem and hence write the doubly stochastic matrix H as a convex combination of permutation matrices

$$
\mathrm{H}=\left(\begin{array}{ccc}
0 & 0.5 & 0.5 \\
0.8 & 0.2 & 0 \\
0.2 & 0.3 & 0.5
\end{array}\right)
$$

d) A company has an annual demand of 16000 units of item $L$ each costing sh. 200. The cost per order is sh. 1000 while the cost of capital is $24 \%$. To purchase 10,000 or more units the price is sh.190. Justify why the management should buy with or without the discount.
(6 marks)
e) A lorry can carry 4 tones, there are 3 types of objects that can be loaded. Their values and weights (tones) are given below.

| Item (i) | $\mathrm{V}_{\mathrm{i}}$ | $\mathrm{W}_{\mathrm{j}}$ |
| :--- | :--- | :--- |
| 1 | 31 | 2 |
| 2 | 47 | 3 |
| 3 | 14 | 1 |

Determine the load which maximizes the value of the objects in the lorry
f) Highlight two negative impacts of traffic jam

## QUESTION TWO (20 MARKS)

a) Determine the maximum flow and the minimum cut in the following network (10 marks)

b) Using the project activities details recorded below
i. Draw the network to represent the project and mark the critical path
ii. Compute the total float for the non critical activities
iii. Determine the probability that the project is completed within 26 weeks
(10 marks)

| Activity | Preceding <br> activity | Duration <br> (weeks) | Standard <br> deviation |
| :--- | :--- | :--- | :--- |
| A | ---- | 5 | 1.5 |
| B | ---- | 6 | 2.0 |
| C | A | 7 | 2.5 |
| D | A | 4 | 1.0 |
| E | A,B | 2 | 0.5 |
| F | C,D,E | 4 | 1.5 |
| G | D,E | 10 | 3.0 |
| H | F,G | 3 | 1.5 |

## QUESTION THREE (20 MARKS)

a) The figure below represents four road junctions A, B, C and D


Using the figure above
i. Construct the mathematical model to represent the traffic flow
ii. Determine the minimum flow a long AB and the flows a long $\mathrm{DB}, \mathrm{DC}$ and AC at that moment.
b) Given the spot speeds are $50,80,60,55$ and 45 , determine the time mean speed and space mean speed
c) Distinguish between the critical path method (CPM) and project evaluation and review technique (PERT)

## QUESTION FOUR (20 MARKS)

a) The following details relate to item K10 an input in a production process. Normal consumption is $100,000 \mathrm{~kg}$ per week, maximum consumption is $150,000 \mathrm{~kg}$ per week, minimum consumption is $50,000 \mathrm{~kg}$ per week, re-order quantity is $600,000 \mathrm{~kg}$ and re-order period is 4-6 weeks. Determine;
i. Re-order level
ii. Average stock level

A company has 5 workers and 5 jobs. From the past experience workers can perform specific jobs as summarized below

| Worker | Job performs |
| :--- | :--- |
| 1 | 2 |
| 2 | 1,4 |
| 3 | 1,2 |
| 4 | $1,2,3,4$ |
| 5 | 3,5 |

i. Represent the above information in a graph and a matrix
ii. Determine the maximal match

A firm has five positions and five applicants, given the utility matrix A, determine the optimal assignment

$$
A=\left(\begin{array}{lllll}
7 & 2 & 8 & 4 & 3 \\
5 & 4 & 6 & 3 & 3 \\
6 & 3 & 7 & 4 & 5 \\
5 & 2 & 5 & 2 & 4 \\
3 & 0 & 4 & 3 & 1
\end{array}\right)
$$

## QUESTION FIVE (20 MARKS)

a) Highlight four conditions that may necessitate the use of simulation in modeling a system behavior (4 marks)
b) The Kulima limited company has designed a new pesticide whose production requires mainly two ingredients X 1 and $\mathrm{X}_{2}$. With the production function $y=\sqrt{x_{1}} x_{2}$ where $x_{1}$ and $x_{2}$ are the units of ingredient 1 and 2 respectively required to produce one sachet of $y$. The price of each sachet and the cost of the ingredients are random variables such that

| SP (y) | Probability |
| :--- | :--- |
| 4000 | 0.15 |
| 4500 | 0.35 |
| 5000 | 0.20 |
| 5500 | 0.30 |


| Cost (x1) | Probability |
| :--- | :--- |
| 1000 | 0.1 |
| 1500 | 0.05 |
| 2000 | 0.35 |
| 2500 | 0.50 |


| Cost (x2) | Probability |
| :--- | :--- |
| 1500 | 0.20 |
| 2000 | 0.25 |
| 2500 | 0.15 |
| 3000 | 0.40 |

i. Given that the daily usage of x 1 and x 2 are set at 250 and 360 units respectively.

Determine the expected profit of the company.
(6 marks)
ii. Simulate the company's profit for 10 days using the random numbers;
$58,71,96,30,24,18,09,24,18,46,23,34,27,85,13,99,24,44,49,79,49,74,16,32,23,02,56,88,87$
,59.

