Machakos university
School of pure and applied sciences
Department of mathematics and statistics
First second semester examination for certificate in B.C.E and plumbing.
Mathematics

Instructions

Answer all the questions
show your working clearly.
Question one
a) Solve the following equations (16 marks)
i) $\quad 2^{2 x-3}=4^{x+3}$
ii) $\quad \frac{4^{2 x} \times 8^{x}}{2^{x}}=64$
iii) $\quad \log (x+6)-\log (x-3)=1$
iv) $2 x-3 y=7$
$4 x+3 y=5$
b) Determine the LCM of36,45 and 60 ( 4 marks)

## Question two

a) Evaluate,
i) $\log 96+3 \log 5-\log 12$
ii) $\frac{1}{2}\left\{\frac{3}{5}+\frac{1}{4}\left(\frac{7}{3}-\frac{3}{7}\right)\right\}$ of $1 \frac{1}{2} \div 5(10$ marks $)$
b) Make I the subject of the formula

$$
\frac{2 l}{l+r c R}=m
$$

Hence calculate the value of $L$ when $m=\frac{1}{2} r=3, c=4, R=5$
c) Express 3.280843 m in
i) $\quad \mathrm{Cm}$
ii) Km
iii) Correct to 2 s.f. (3marks)

Question three
a) The fourth term of an A.P is 14 and the sum of the first six terms is 69 . Determine the:
i) First term
ii) Common difference
iii) Sum of the first sixteen terms. (9marks)
b) If the median of the numbers $25, x, 16,12,24$ and 14 is 18 , find $x$.
c) The table below shows the number of goals scored by a team in 15 matches.

| score | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| frequency | 1 | 0 | 3 | 2 | 5 | 3 | 1 |

Determine
i) The mean
ii) The mode
iii) The median

## Question four

a) Solve the following equations
i) $x^{2}+15 x+50=0$
ii) $\quad 3^{x+1}=2^{2 x-3}$ correct to 2 decimal place
b) John borrowed sh 75,000 for two years. The rate of simple interest for the first year was $9.75 \%$, but for the second year the rate increased to $11 \%$. How much more interest he paid in the second year than in the first year ( 5 marks)

Simplify
i) $\frac{2 x-3}{3}-\frac{x-2}{2}-\frac{1-x}{4}$
ii) $\log _{e} 3$

Question five
a) Express the first quantity as a fraction of the second quantity (6marks)
i) 45 seconds: I hour
ii) $450 \mathrm{~g}: 2 \mathrm{~kg}$
b) Express 0.18 as a fraction (3marks)
c) Draw the graph of $y=-x^{2}+5 x+2$ for values of $x$ from -3 to 7 ; hence use the graph to solve the following equations (11marks)

$$
\begin{aligned}
& -x+5 x+2=0 \\
& 3+x-x^{2}=0
\end{aligned}
$$

