# MACHAKOS UNIVERSITY 

University Examinations 2018/2019

SCHOOL OF PURE AND APPLIED SCIENCES
DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE FOURTH YEAR SUPPLEMENTARY EXAMINATION FOR BACHELOR OF SCIENCE (MATHEMATICS AND STATISTICS) SMA 366: QUALITY CONTROL METHODS

## INSTRUCTIONS:

## Answer question one and any other two

QUESTION ONE (30 MARKS)
a) Distinguish the following terms as used in statistical quality control
i. Sampling and Census
ii. Control limits and Tolerance limits
iii. Process control and product control
b) A quality control officer in NCPB store claims that $70 \%$ of the cereals in the store are bad. A random sample of 50 bags showed that 35 of them were bad. Are these sample results consistent with the claim of the officer? Use $\alpha=0.05$
c) The table below shows the mean and range for 10 samples each of size 5

| Sample no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Range | 11.4 | 12.0 | 11.0 | 11.8 | 11.2 | 9.8 | 10.6 | 9.8 | 10.8 | 10.2 |
| Mean | 7 | 4 | 8 | 5 | 7 | 4 | 8 | 4 | 7 | 9 |

By using mean and range charts determine whether the process is in control (6 marks)
d) By citing examples distinguish between the control charts for variables and attributes
e) During an examination of equal length of a piece of cloth the following number of defects were observed; $2,3,4,0,5,6,7,4,3,2$.

Draw the control chart for the number of defects and commend on the state of the process
(6 marks)
f) Distinguish between the random variation and assignable variations by giving examples
(4 marks)

## QUESTION TWO (20 MARKS)

a) Distinguish between the producers risk and consumer's risk (4 marks)
b) Given $\mathrm{N}=500, \mathrm{n}=150$ and $\mathrm{c}=3$ construct OC curve for $0.01 \leq \mathrm{p} \leq 0.06$ based on Poisson distribution
c) In a random sample of 100 items taken from machine $A, 60$ are found to be defective. In another sample of 200 items taken from machine $B, 100$ items are found to be defective. Do the data reveal significant difference between the two machines as far as the quality output is concerned?

## QUESTION THREE (20 MARKS)

a) Discuss briefly the meaning of single, double and multiple acceptance sampling plans
b) Highlight three advantages of Cusum control charts over Shewart control charts
c) The following shows the thickness of steel tubes, whose target thickness $\left(\mu_{0}\right)$ is 10 cm . construct the Cusum chart using the data and commend on the process status.

| Sample No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| X in cm | 9.45 | 7.99 | 9.29 | 11.66 | 12.16 | 10.18 | 8.04 | 11.46 | 9.20 | 10.34 |
| Sample No. | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| X in cm | 9.03 | 11.47 | 10.51 | 9.40 | 10.08 | 9.37 | 10.62 | 10.31 | 8.52 | 10.84 |
| Sample No. | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| X in cm | 10.90 | 9.33 | 12.29 | 11.50 | 10.60 | 11.08 | 10.38 | 11.62 | 11.31 | 10.52 |

## QUESTION FOUR (20 MARKS)

a) A manufacturer of electric gadgets has known from experience that $3 \%$ of the gadgets produced are defective, if random sample of 300 gadgets is examined determine the probability that the proportion defective is between 0.025 to 0.035
(4 marks)
b) Discuss any five dimensions of quality characteristics in production industry ( 10 marks)
c) Highlight six quality characteristics of a quality control officer
(6 marks)

## QUESTION FIVE (20 MARKS)

a) Differentiate the following terms as apply in social research.
i. Type I and Type II error
ii. Two tailed and one tailed test
iii. Descriptive and inferential statistics
iv. Null hypothesis and Alternative hypothesis
b) The following information relates to the lifespan electric bulbs manufactured by two companies A and B:

|  | Company A | Company B |
| :--- | :---: | :---: |
| Mean life (in hours) | 1300 | 1288 |
| Standard deviation (in hours) | 82 | 93 |
| Sample size | 100 | 100 |

Which brand of bulbs would you recommend for a client taking a risk of 5\%?
(6 marks)
c) Two different types of machines A and B products had the following number of defective items per run

| Runs | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Defectives from machine A | 8 | 12 | 13 | 9 | 3 | - | - |
| Defectives from machine B | 10 | 8 | 12 | 15 | 6 | 8 | 11 |

Determine whether the two machines differ significantly with regard to their effect in producing defective items at $\alpha=5 \%$

