



MACHAKOS UNIVERSITY

University Examinations for 2022/2023 Academic Year

SCHOOL OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

THIRD YEARSEMESTER EXAMINATION FOR
BACHELOR OF SCIENCE (TELECOMMUNICATION AND INFORMATION
TECHNOLOGY)

SPH307 DIGITAL ELECTRONICS

DATE:

TIME:

INSTRUCTIONS

ANSWER QUESTION ONE AND ANY OTHER TWO QUESTIONS

QUESTION ONE (COMPULSORY) (30 MARKS)

- a) Find the decimal equivalent of binary number, 1 1 0 1 1 0 0 1. 0 101 0 (3marks)
- b) Convert the following numbers from binary to hexadecimal
100100011
1111000000001101 (4 marks)
- c) Represent the decimal number 5,137 in (i)BCD, (ii) excess -3 code (2 marks)
- d) Simplify the following expression using Boolean algebra laws and rules and implement the simplified expression using logic gates.

$$F = xy + xyz + xy\bar{z} + \bar{x}yz \quad (5 \text{ marks})$$

- e) A 4-bit binary number is applied to a circuit on four lines A, B, C, D. The circuit has a single output, F, which is true if the number is in the range three to twelve, inclusive.
- (i) Draw a truth table to represent the problem (3 marks)
- (ii) Use the K-map to obtain a simplified expression for the function (4 marks)
- (iii) Construct a circuit to implement the simplified expression in (ii) above using NAND gate only. (3 marks)

- e) Express the complement of the following functions in sum-of-min-terms form:
 i) $F(A, B, C, D) = \sum(3, 5, 9, 1, 15)$ ii) $F(x, y, z) = \prod(2, 4, 5, 7)$ (2 marks)
- f) Draw the multi-level NAND circuit for the given expression (4 marks)
- $$w(x + y + z) + xyz$$

QUESTION TWO (20MARKS)

- a) Convert the following numbers with the indicated bases to decimal (8 marks)
- i) $(4310)_5$ ii) $(198)_{12}$ iii) $(735)_8$ iv) $(525)_6$
- b) Demonstrate the validity of the following identities by means of truth tables (12 marks)
- DeMorgan's theorem for three variables $(x + y + z)' = x'y'z'$ and $(xyz)' = x' + y' + z'$
 - The distributive law $x + yz = (x + y)(x + z)$
 - The associative law $x + (y + z) = (x + y) + z$

QUESTION THREE (20 MARKS)

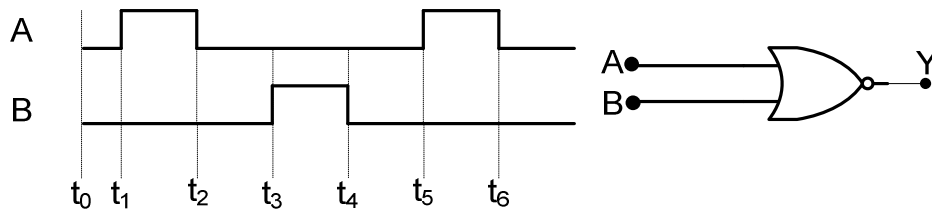
- a) Draw a NAND logic diagram that implements the complement of the given function.
 $F(A, B, C, D) = \sum(0, 1, 2, 3, 4, 8, 9, 12)$ (10 marks)
- b) Design a combinational circuit with three inputs and one output (10 marks)
- The output is 1 when the binary value of the input is less than 3. The output is 0 otherwise
 - The output is 1 when the binary value of the input is an odd number.

QUESTION FOUR [20MARKS]

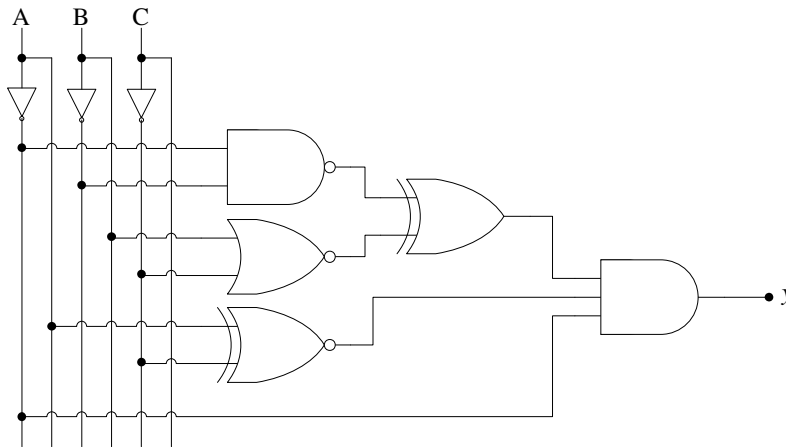
- a) A majority circuit is a combinational circuit whose output is equal to 1 if the input variable has more 1's than 0's. The output is 0 otherwise. Design a three-input majority circuit by finding the circuit truth table, Boolean equation and a logic diagram (10 marks)
- b) Prove the following Boolean identity
 $(A+B)(A+\bar{B})(\bar{A}+C) = AC$ (4 marks)
- c) With the aid of logic symbols and truth tables, explain the operation of the following two-input gates.
 (i) NAND
 (ii) XOR (6 marks)

QUESTION FIVE (20MARKS)

- a) The figure below shows the two waveforms applied to the NOR gate. Determine the resulting output waveform. (4 marks)



- b) Differentiate between combinational and sequential circuits. (5 marks)
- c) Determine the Boolean expression and the truth table for the output of the logic circuit shown below. (4 marks)



- d) Simplify the following Boolean expression to a minimum number of literal hence implement the logic gate
- e) $ABC\bar{C} + \bar{A}BC + ABC + \bar{A}B\bar{C}$ (4 marks)
- f) Use 2's complement to subtract 1101_2 from 1010_2 (3 marks)