



MACHAKOS UNIVERSITY

University Examinations 2017/2018

SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS AND STATISTICS

SUPPLEMENTARY EXAMINATION FOR DIPLOMA IN EDUCATION

SMA 0201 VECTOR ANALYSIS

DATE:

TIME:

INSTRUCTIONS TO CANDIDATES

Answer Question One and Any Other Two Questions

QUESTION ONE (30 MARKS)

- a) (i) Define a vector (1 mark)
(ii) Define a scalar (1 mark)
(iii) List three laws of algebra (3 marks)
(iv) Define a unit vector (1 mark)
(v) Define a vector field (1 mark)
- b) If $\mathbf{A} = 2\mathbf{i} + 3\mathbf{j} - 2\mathbf{k}$ and $\mathbf{B} = 4\mathbf{i} - 2\mathbf{j} + 4\mathbf{k}$. Find;
- (i) $\mathbf{A} \cdot \mathbf{B}$ (2 marks)
(ii) $\mathbf{B} \cdot \mathbf{A} + 2\mathbf{B}$ (3 marks)
(iii) The angle between the vectors $\mathbf{A} = 3\mathbf{i} + 2\mathbf{j} - 6\mathbf{k}$ and $\mathbf{B} = 4\mathbf{i} - 3\mathbf{j} + \mathbf{k}$ (3 marks)
- (c) If $\mathbf{A} + \mathbf{B} = 3\mathbf{i} + \mathbf{j} - 3\mathbf{k}$, $\mathbf{A} - \mathbf{B} = \mathbf{i} - 7\mathbf{j} + \mathbf{k}$, then find the value of $(\mathbf{A} + \mathbf{B}) \times (\mathbf{A} - \mathbf{B})$ (3 marks)
- d) Find the projection of a vector $\mathbf{A} = \mathbf{i} - 2\mathbf{j} + \mathbf{k}$ on vector $\mathbf{B} = 4\mathbf{i} - 4\mathbf{j} + 7\mathbf{k}$ (3 marks)

f) If the vector $\mathbf{A} = 5t^2\mathbf{i} + t\mathbf{j} - t^3\mathbf{k}$ and $\mathbf{B} = \sin t\mathbf{i} - \cos t\mathbf{j}$, find:

(i) $\frac{d}{dt} \mathbf{A} \cdot \mathbf{B}$ (2 marks)

(ii) $\frac{d}{dt} \mathbf{A} \times \mathbf{B}$ (2 marks)

(iii) $\frac{d}{dt} \mathbf{A} \cdot \mathbf{A}$ (2 marks)

QUESTION TWO (20 MARKS)

a) If $\mathbf{A} = (2x^2y - x^4)\mathbf{i} + (e^{xy} - y \sin X)\mathbf{j} + (x^2 \cos y)\mathbf{k}$. Find

(i) $\frac{\partial A}{\partial x}$ (1 mark)

(ii) $\frac{\partial A}{\partial y}$ (1 mark)

b) If $\mathbf{A} = \cos xy\mathbf{i} + (3xy - 2x^2)\mathbf{j} - (3x + 2y)\mathbf{k}$ find

(i) $\frac{d\mathbf{A}}{dx}$ (1 mark)

(ii) $\frac{d\mathbf{A}}{dy}$ (1 mark)

(iii) $\frac{d^2\mathbf{A}}{dx^2}$ (1 mark)

(iv) $\frac{d^2\mathbf{A}}{dy^2}$ (1 mark)

(v) $\frac{d^2\mathbf{A}}{dydx}$ (2 marks)

(vi) $\frac{d^2\mathbf{A}}{dxdy}$ (2 marks)

QUESTION THREE (20 MARKS)

(a) if a particle moves along a curve whose parametric equations are
 $x = e^{-t}$, $y = 2\cos t$, $z = 2 \sin 3t$

(i) Determine the velocity and acceleration at any time (2 marks)

(ii) Find the magnitude of the vector and acceleration at $t=0$ (2 marks)

(b) Determine $\Delta\Theta$ if $\Theta = z^2 \cos(xy - \pi/4)$ and find its value at the point $(1/\sqrt{2}, 1)$ (3 marks)

(c) Find the directional derivative of $\Theta = x^2yz + 4xz^3 + xyz$ at $(1, 2, 3)$ in the direction

Of $2\mathbf{i} + \mathbf{j} - \mathbf{k}$ (3 marks)

QUESTION FOUR (20 MARKS)

(a) If $\mathbf{A} = (3x^2 + 6y)\mathbf{i} - 14yz\mathbf{j} + 20xz^2\mathbf{k}$,

Evaluate $\int \mathbf{A} \cdot d\mathbf{r}$ from $(0, 0, 0)$ to $(1, 1, 1)$ along the following parts

(i) $X=t$, $y=t^2$, $z=t^3$ (2 marks)

(ii) The straight line joining $(0, 0, 0)$ and $(1, 1, 1)$. (2 marks)

(iii)

- (b) Evaluate $\int_C \mathbf{A} \cdot d\mathbf{r}$ where C is the curve $y=x^3$ in the xy- p. plane from the point (1,1) to (2,8) if $\mathbf{A}=(5xy-6x^2)\mathbf{i} + (2y-4x)\mathbf{j}$ (3 marks)
- (c) Evaluate the integral from $\int_1^3 \int_{1/2x}^{4x} 2xy \, dy \, dx$ (3 marks)

QUESTION FIVE (20 MARKS)

- (a) Evaluate $\int_0^1 \int_0^{2x} \int_{x-y}^{x+y} 30xy \, dz \, dy \, dx$ (4 marks)
- (b) State the Green's Theorem (2 marks)
- (c) State the stoke's Theorem (2 marks)
- (d) State the Gauss-Divergence Theorem (2 marks)