



# Machakos University

University Examination for 2017/2018

## SCHOOL OF ENGINEERING AND TECHNOLOGY

### DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

### SECOND SEMESTER EXAMINATION FOR BACHELOR OF SCIENCE IN ELECTRICAL AND ELECTRONICS ENGINEERING

#### EEE 518: DIGITAL IMAGE PROCESSING

DATE:

TIME: 2 HRS

#### QUESTION ONE (30 Marks)

- a) Name and explain the three types of connectivity (6 marks)
- b) Write down the formula for calculating  $D_4$  (City block distance) and  $D_8$  distance (Chess board distance) (2 marks)
- c) Consider the image below. Show the result of a  $3 \times 3$  median filtering if the following masks are used. A '0' in a mask position means that the corresponding pixel is not used for calculating the median.

|   |   |   |   |
|---|---|---|---|
| 3 | 5 | 8 | 4 |
| 9 | 1 | 2 | 9 |
| 4 | 6 | 7 | 3 |
| 3 | 8 | 5 | 4 |

(a) Fig1.1

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
| 1 | 1 | 1 |
| 1 | 1 | 1 |

Fig.1.2

|   |   |   |
|---|---|---|
| 0 | 1 | 0 |
| 1 | 1 | 1 |
| 0 | 1 | 0 |

Fig.1.3

(5 marks)

- d) Consider the histogram [2,2,4,8,16,32,64,128] where the number of gray levels is 8.
- Determine the output histogram of histogram equalization
  - Using the result in (i), explain how histogram equalization enhances the contrast of an image

(4 marks)

- e) (i) Explain the need of image segmentation  
(ii) Describe the seeded segmentation method

(6 marks)

- f) (i) Using relevant equations, describe the relationship between the average value of an image and its DFT  
(ii) For the image in Fig. 1.4, illustrate the relationship stated in (i)

|   |   |   |   |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 |
| 0 | 0 | 0 | 0 |

Fig.1.4

(7 marks)

### QUESTION TWO(20 Marks)

- a) Consider a  $M \times N$  pixel gray level image  $f(x, y)$  which is zero outside  $0 \leq x \leq M - 1$  and  $0 \leq y \leq N - 1$ . The image intensity is given by the following relationship

$$f(x, y) = \begin{cases} c & y = y_0 \\ 0 & \text{otherwise} \end{cases}$$

Where  $c$  is a constant value between 0 and 255 and  $y_0$  is a constant between 0 and  $N - 1$ .

- Plot the image intensity
- Find the  $M \times N$ -point Discrete Transform of  $f(x, y)$ . Plot its magnitude spectrum.
- Compare the plots found in (i) and (ii) above

$$\left[ \sum_{k=0}^{N-1} a^k = \frac{1-a^N}{1-a} \quad |a| \leq 1 \right]$$

(10 marks)

- b) (i) Obtain the discrete Fourier transform  $H(u, v)$  of  $h(x, y) = \begin{cases} 1 & x = 0 \ y = 0 \\ 2 & x = 0 \ y = 1 \\ 1 & x = 0 \ y = 2 \end{cases}$

(ii) Determine the values of  $v$  for which  $H(u, v) = 0$ .

(10 marks)

### QUESTION THREE(20 Marks)

a) Describe the following filtering methods

- i. Inverse filter
- ii. Wiener filter

(6 marks)

b) (i) Derive the transfer function  $W(u, v)$  of the Wiener filter

(ii) Show the relationship between the Wiener filter and the

- I. Inverse filter
- II. Pseudo inverse filter

(14 marks)

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**QUESTION FOUR(20 Marks)**

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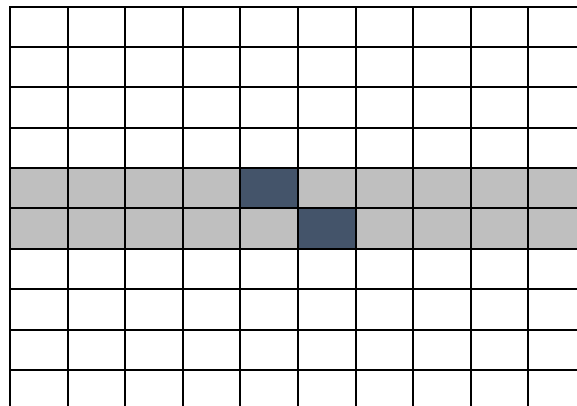
a) Write down three image data compression techniques

( 3 marks)

b) Figure 1 shows  $10 \times 10$  image with 3 different gray levels (black, grey and white)

- i. Derive the probability of appearance (that forms the histogram) for each intensity (grey) level. Determine the entropy of the image.
- ii. Derive the Huffman code
- iii. Calculate the average length of the fixed length code and that of the derived Huffman code.
- iv. Calculate the image size (in bits) between using the fixed length coding and Huffman coding. Calculate the relative coding redundancy.

(17 marks)



**Figure 4.1**

### QUESTION FIVE(20 Marks)

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a) Describe the role of histogram in image processing

**(3 marks)**

b) (i) Figure 5.1 shows a 3-bit  $4 \times 4$  image perform histogram equalization and find the resulting image

|   |   |   |   |
|---|---|---|---|
| 0 | 0 | 0 | 4 |
| 1 | 1 | 1 | 5 |
| 1 | 2 | 2 | 7 |
| 2 | 2 | 2 | 7 |

Figure 5.1

(ii) A  $5 \times 5$  image is to be obtained from a  $3 \times 3$  image given in Figure 5.2 . Explain the nearest neighbor and bilinear transformation and show how the resulting  $5 \times 5$  will look for each of the interpolation methods.

|   |   |   |
|---|---|---|
| 0 | 2 | 4 |
| 2 | 4 | 6 |
| 4 | 6 | 8 |

Fig. 5.2

**(7 marks)**

c) Apply toboggan contrast enhancement to the image in Fig. 5.3. The gradient magnitude of each pixel location is given in Fig.5.4. Show all intermediate steps. **(10 marks)**

|   |   |   |   |
|---|---|---|---|
| 4 | 4 | 3 | 2 |
| 4 | 7 | 6 | 1 |
| 2 | 7 | 6 | 2 |
| 0 | 1 | 0 | 2 |

Figure 5.3

|    |    |    |    |
|----|----|----|----|
| 12 | 14 | 23 | 13 |
| 16 | 11 | 21 | 18 |
| 21 | 24 | 23 | 13 |
| 12 | 21 | 20 | 10 |

Figure 5.4