



MACHAKOS UNIVERSITY

University Examinations 2018/2019

SCHOOL OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF MECHANICAL AND MANUFACTURING ENGINEERING

THIRD YEAR SPECIAL/SUPPLEMENTARY EXAMINATION FOR

BACHELOR OF SCIENCE IN MECHANICAL ENGINEERING

EMM 312 FLUID MECHANICS III

DATE: 23/7/2019

TIME: 2.00-4.00 PM

INSTRUCTIONS:

Answer Question One and Any Other Two Questions

QUESTION ONE (COMPULSORY QUESTION) [30 MARKS]

- a) Define the term
- i. Specific Energy (2 marks)
 - ii. Critical depth (2 marks)
- b) i for an open rectangular channel of critical depth D_c , breadth B and critical velocity V_c , show that;

$$D_c = 2 \left[\frac{V_c^2}{2g} \right]$$

Where; g = acceleration due to gravity (4 marks)

- ii in a rectangular channel the specific energy of flow is 1.8m. calculate
- the critical depth (2 marks)
 - discharge per unit width of this depth (2 marks)
- c) i derive the Chezy formula for an open rectangular channel using usual notation and explaining the meaning of all the symbols (4 marks)
- assume that the resistance to flow is proportional to the square of the velocity of flow.

- ii an open channel is trapezoidal shaped in cross-section with a bottom width of 45m slopes of 1 vertical to $1\frac{1}{2}$ horizontal. The bed slope is 1 in 180 and the depth of water 1.15m calculate the volumetric flow rate if the Chezy constant $c = 40$ (6 marks)
- d) i) Derive an expression for discharge over a flat-topped broad crested weir forming a spillway to a large reservoir. (3 marks)
- ii) Show that the maximum discharge Q_{max} is given by;
- $$Q_{max} = Cd1.706LH^{\frac{2}{3}}$$
- Where Cd =coefficient of discharge
 L =breadth of the reservoir
 H =height
 $G=9.81\text{m/s}^2$ (2 marks)
- iii) a flat topped broad crested weir is designed for a maximum discharge of $7.03\text{m}^3/\text{sec}$. calculate the appropriate water level upstream of the weir if the width is 15m and the coefficient of discharge is 0.6 (3 marks)

QUESTION TWO (20 MARKS)

- a) Describe the phenomenon of water hammer in a pipeline resulting from the complete and instantaneous closure of a valve; friction being neglected (3 marks)
- b) Explain using suitable diagram the pressure variation with time at a point in the immediate neighborhood of the valve and at a point half-way the length of the pipe (4 marks)
- c) Show that the pressure rise at the valve (P) is given by;

$$P = V \sqrt{\frac{e}{\frac{1}{K} + \frac{d}{4tE} (5 - \nu)}}$$

Where

V =velocity of flow before closure of the valve

d = diameter of the pipe

t = pipe thickness

E = Young Modulus of elasticity of the pipe

K = Bulk Modulus of water

ν = poisson's ratio

ρ = mass density of valve (10 marks)

- d) Calculate the maximum permissible discharge in a 160mm diameter pipe, if the pressure is not to exceed 1500 kN/m^2 , when the outlet is suddenly closed;

Assume: the pipe is rigid

For water $K=2.07 \times 10^9 \text{ N/m}^2$ and
density = 10^3 kg/m^3 .

(3marks)

QUESTION THREE (20 MARKS)

- a) Show that the compressible adiabatic mass flowrate ($\dot{M}$) through a horizontal venturimeter is given by;

$$\dot{M} = \frac{C_d P_1 A_1}{RT_1} \sqrt{\frac{2 \left(\frac{\gamma}{\gamma-1} \right) RT_1 \left[1 - \frac{\gamma-1}{\gamma} \right]}{\left[\frac{A_1}{A_2} \right]^2 \left(\frac{1}{r_p} \right)^{\frac{2}{\gamma}} - 1}}$$

Where;

C_d = coefficient of discharge

P_1 = absolute pressure at inlet

A_1 = x-sectional area of inlet pipe

T_1 = absolute temperature at entry

R = universal gas constant

$$r_p = \frac{P_2}{P_1}$$

γ = adiabatic expansion) compression ratio (8 marks)

- b) It is required to design a venturimeter so that when the flow rate is 1.6 kg/sec , the pressure ratio is 0.75 , the other parameters being as follows; $C_d = 0.96$, $R = 0.287 \text{ kJ/kgK}$, $P_1 = 150 \text{ kN/m}^2$ also the $T_1 = 200^\circ\text{C}$, $d_1 = 0.25 \text{ m}$ and $\gamma = 1.4$. Calculate the throat diameter required.

Assume $\left(\frac{\gamma}{\gamma-1} \right) \frac{P}{\rho} + \frac{v^2}{2} = \text{constant}$ (12 marks)

QUESTION FOUR (20 MARKS)

- a) Prove that the maximum continuous discharge of air through a small orifice fitted in the side of a large vessel takes place when the pressure in the throat is 0.528 of the pressure inside the vessel.

$$\text{Assume } \left(\frac{\gamma}{\gamma-1}\right) \frac{P}{\rho} + \frac{v^2}{2} = \text{constant} \quad (10 \text{ marks})$$

- b) Determine the mass flow rate through an orifice of 225mm diameter connected to a large tank if the air in the tank is at 140kN/m² absolute and the barometric pressure 100kN/m²
Assume; air temperature is 20°C

$$R = 0.287 \text{ kJ/kgK}$$

$$\gamma = 1.4 \quad (10 \text{ marks})$$

QUESTION FIVE (20 MARKS)

- a) What is a shockwave? (2 marks)
- b) Distinguish between a normal and oblique shock wave (3 marks)
- c) A normal shock wave moves through still air (101.0kN/m² pressure and 298°C temperature) with a constant velocity of 1500m/se

Calculate;

- i) Velocity of air below the wave (5 marks)

- ii) Static pressure (5 marks)

- iii) Temperature (5 marks)

Assume $R = 292.7 \text{ kJ/kgK}$