



MACHAKOS UNIVERSITY

University Examinations 2021/2022 Academic Year

SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS AND STATISTICS

FOURTH YEAR FIRST SEMESTER EXAMINATION FOR

BACHELOR OF SCIENCE (STATISTICS AND PROGRAMMING)

SAC 401: SURVIVAL MODELS

DATE: 29/8/2022

TIME: 2.00-4.00 PM

INSTRUCTION:

Answer Question One and Any Other Two Questions

QUESTION ONE (COMPULSORY) (30 MARKS)

- a) Differentiate the following terms as they apply in survival models
- i. Right censoring and left censoring (2 marks)
 - ii. Interpolation and Extrapolation point estimate (2 marks)
 - iii. Transactional Risk Exposure and Economic Risk Exposure (2 marks)
- b) Given that a survival density function takes the form $f(t) = \lambda e^{-\lambda t}$; $t > 0$, $\lambda > 0$ determine;
- i. $s(t)$ (3 marks)
 - ii. $h(t)$ (3 marks)
- c) The population extract of a town where census is taken once in every 10 years is given below.

Year	1981	1991	2001	2011
Population	35000	42000	58000	84000

- Estimate the population in the year 1985 (8 marks)
- d) Determine the amount of an annuity of Ksh 30,000 every year for 10 years if the interest rate is 8% per annum compounded quarterly. (5 marks)

- e) Given below is a life table extract from a certain county hospital in Kenya.

Age (Years)	<1	1-5	6-10	11-15	
${}_n l_x$	10,000	9,885	9,339	8,887	
${}_n d_x$	115	546	452	237	

Using the table data determine the following;

- ${}_5 P_{10}$ (2 marks)
- ${}_5 L_{10}$ (3 marks)

QUESTION TWO (20 MARKS)

- a) An investor is indifferent on which investment option to invest his Ksh 450,000 among the following options;

Options	A	B	C
Risk of Loss (%)	5	8	12
Returns (%)	10	13	15

- Advise the option with the least risk exposure (3 marks)
 - Explain any two methods of managing business risk exposures (2 marks)
- b) The following is an extract of the life table from an African country whose *radix* is 10,000.

Age (yrs)	<1	1-9	10-19	20-29	30-39	40-49	50-59	60-69	70>
l_x	10000	9077	8288	7669	7146	6322	5173	3620	1289
${}_n d_x$	923	789	619	523	824	1149	1553	2331	1289

For each age group determine;

- The probability of surviving (${}_n P_x$) (5 marks)
- Life expectancy (e_x) (10 marks)

QUESTION THREE (20 MARKS)

- a) The following data relates to the child's age in years and his weight in kilograms.

Age (Years)	5	6	9	11
Weight (kg)	12	13	14	16

Estimate his weight at 10 years.

(5 marks)

- b) The data below relates to the time to death after a kidney transplant in one of the referral hospitals. The patients were categorised into male and females.

Gender	Time to discharge in years				
Males (M)	7	13	18	19+	20
Females(F)	15	17	25	27+	35+

Test the hypothesis at $\alpha = 0.05$ that;

$$H_0: S_M(t) = S_F(t)$$

$$\text{Versus } H_1: S_M(t) \neq S_F(t)$$

(15 marks)

QUESTION FOUR (20 MARKS)

- a) Distinguish between retrospective policy value and prospective policy value (6 marks)
- b) Suppose that 5000 lives were selected for life insurance at age 30. If $q_{[30]+k} = \frac{1.1}{50}$ for $k=0,1,2,3,4,5,\dots$ determine the numbers of deaths between the age of 30 to 32. (6 marks)
- c) A medical insurance company had her clients' age distribution as summarised below in a certain centre.

Age (years)	0-19	20-39	40-59	60-79	80-99
No. Insured	41	62	65	50	17

Estimate the number of insured whose age is greater than 70 years.

(8 marks)

QUESTION FIVE (20 MARKS)

- a) Determine ${}_{20}V_{45}$ given that $P_{45} = 0.014$, $P_{\frac{1}{45:20}} = 0.22$ and $P_{45:\overline{20}} = 0.030$ (5 marks)
- b) A group of 15 laboratory rats were injected with a new pests control drug and observed over the following 30 days. The turn of events is as summarised below.

Death day	3	4	11	21	26
Rat number	4	13	6 & 9	10	5

The research also noted the following; On the 6th day rat number 7 escaped from the cage and rat number one was killed by the others on the 17th day. Rat number 8 and 12 escaped on the 24th and 25th day respectively. On the 30th day the experiment was closed and remaining rats were set free from the cage.

- i. Represent the information in notation- wise form and then determine; (3 marks)

- ii. The rats' survival function $s(t)$ (6 marks)
- iii. The variance of $s(t)$ (3 marks)
- iv. The 95% CI for $s(t)$ (3 marks)