



MACHAKOS UNIVERSITY

University Examinations 2018/2019

SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

THIRD YEAR SECOND SEMESTER EXAMINATION FOR
BACHELOR OF SCIENCE (STATISTICS & PROGRAMMING)

SST 302: PROGRAMMING LANGUAGE FOR STATISTICS II

DATE: 25/4/2019

TIME: 11:00 – 1:00 PM

INSTRUCTION:

Answer Question **ONE** which is compulsory and any other **TWO** Questions

QUESTION ONE (COMPULSORY) (30 MARKS)

- a) By citing examples differentiate between the discrete random variables and continuous random variables (4 marks)
- b) Highlight three characteristics of the normal probability distribution and write R script for plotting normal curve ranging between -3 to +3 (6 marks)
- c) Suppose that men's neck sizes are approximately normally distributed with a mean of 16.2 inches and variance of 0.81 square inch. Using R script determine the probability that the neck size of a randomly chosen man lies between 13.5 and 18.9 inches. (6 marks)
- d) Write R script for randomly choosing a sample of size five for numbers between 50 and 100 inclusive (3 marks)
- e) Suppose $A = \{2, 3, 5, 7, 11, 13, 17\}$ and $B = \{2, 4, 6, 8, 9, 14, 18\}$ write the R codes for
 - i) $A \cup B$
 - ii) $A \cap B$
 - iii) $A \setminus B$
 - iv) $A' \cup (A \cap B)$ (8 marks)

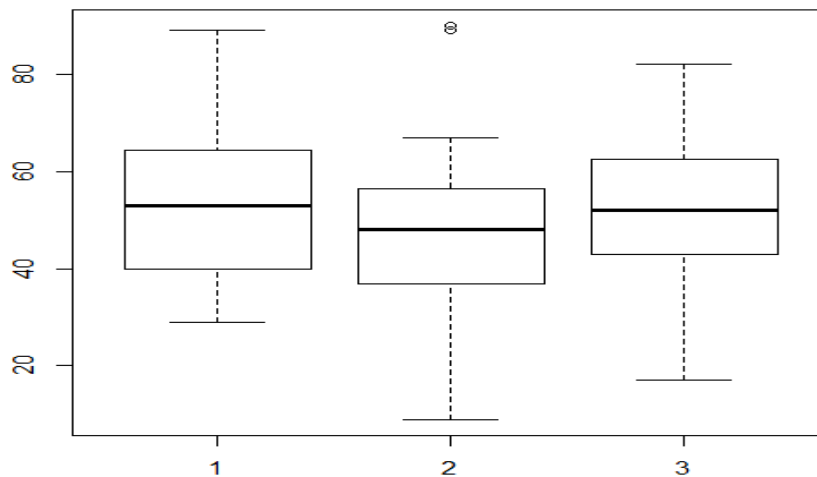
- f) Write the R code for choosing multiples of five from 300 to 375. (3 marks)

QUESTION TWO (20 MARKS)

- a) Suppose in a certain shipment of 250 Pentium processors there are 17 defective processors. A quality control consultant randomly collects 5 processors for inspection to determine whether or not they are defective. By letting X denote the number of defectives in the sample, write the R code for determining $P(x = 3)$ (4 marks)
- b) If X is the number of heads that show up after tossing a fair coin thrice, write the R codes for determine
- i) The sample space
 - ii) the, $E(x)$, $Var(x)$ and standard deviation (x) (8 marks)
- c) Three manufacturing machines A, B and C produces 70%, 20% and 10% of the output in a day. It has being observed that machines A, B and C produce 0.003, 0.004 and 0.005 of defective items respectively. Write the R codes for determining the probability of picking a defective item produced by machine B at random. (8 marks)

QUESTION THREE (20 MARKS)

- a) Write R script for simulating data with 70% chance of choosing “male” for a committee of 20 members. (5 marks)
- b) The figure below gives summary of class 1, 2 and 3 end of term 1, 2019 performance for Tanya Academy.
- i) Write the R script for plotting the figure
 - ii) Use the figure to estimate the; Quartiles, median, the minimum and maximum score for each class.
 - iii) Which class had the highest dispersion? (8 marks)



c) Given the data set below

11, 13, 17, 34, 22, 19, 27, 23, 39, 44, 51, 43, 42, 37, 26 write it in vector form and write the R codes for determining its;

- Arithmetic mean
- Sample Median
- Generic summary for the data and model fits
- Sample quintiles
- Sample variance and standard deviation

(7 marks)

QUESTION FOUR (20 MARKS)

a) A continuous random variable x has a probability function given by:

$$f(x) = \begin{cases} \frac{3}{32} (6x - x^2 - 5) & \text{for } 1 \leq x \leq 5. \\ 0 & \text{elsewhere} \end{cases}$$

Using the R commands

- Show that the function $f(x)$ is a probability density function (p.d.f.)
- Determine the mean and the variance of the random variable x in the probability distribution. (12 marks)

b) Suppose scores in an exam follow normal distribution with mean 80 and standard deviation 5. Using R script determine;

- The minimum score that you should get to be in the top 10%?
- The maximum score that you should get to be in the last 25% (8 marks)

QUESTION FOUR (20 MARKS)

a) Write the R code for

- i) Computing; $2.3^8 + \ln(7.5) - \cos(\pi / \sqrt{2})$
- ii) Generating the even numbers between 30 and 50. (6 marks)

b) Use the R codes

- i) To simulate 20 observations from the binomial distribution with $n = 15$ and $p = 0.2$.
- ii) To estimate the 20th percentile of the gamma distribution with $\alpha = 2$ and $\theta = 10$. (6 marks)

c) A random variable X with PDF given as

$$P(x) = \begin{cases} \frac{1}{\Gamma(p/2)2^{p/2}} x^{p/2} e^{-x/2}, & X > 0 \\ 0 & \text{Otherwise} \end{cases}$$

is said to have a chi-square distribution with

p degrees of freedom. Write the R code used to produce the Chi square distribution figure below (8 marks)

