



MACHAKOS UNIVERSITY

University Examinations for 2019/2020 Academic Year

SCHOOL OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF BUILDING AND CIVIL ENGINEERING

SECOND YEAR SECOND SEMESTER EXAMINATION FOR

BACHELOR OF SCIENCE (CIVIL ENGINEERING)

ECV 209: THEORY OF STRUCTURES II

DATE: 15/12/2020

TIME: 8.30-10.30 AM

INSTRUCTIONS

Answer question **ONE** and any other **TWO** questions

QUESTION ONE (COMPULSORY) (30 MARKS)

- a) Draw the influence lines for the vertical reaction and the reaction moment at support A and the shear and bending moment at point B of the cantilever beam shown in figure 1. (5 marks)

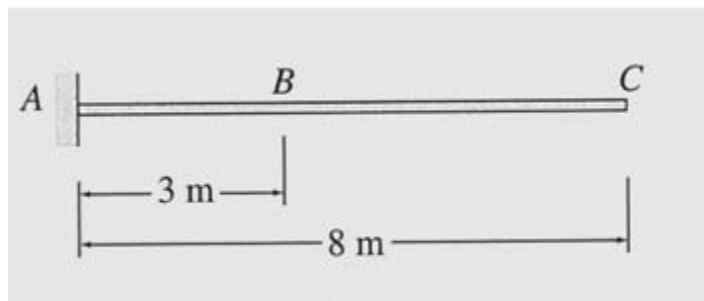


Figure 1

- b) Determine the reactions and draw the shear and bending moment diagrams for the beam shown in figure 2 by the method of consistent deformations (7 marks)

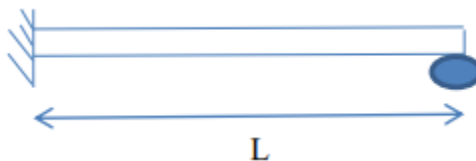


Figure 2

- c) An overhanging beam ABC is loaded as shown in figure 3. Find the slopes over each support and at the right end. (8 marks)

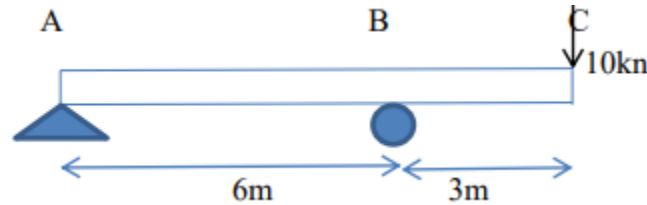


Figure 3

- d) State four classes of arches (4 marks)
- e) Determine the slope and deflection at point B of the cantilever beam shown in figure 4 by the direct integration method. EI is constant. E=200GPa and I= 315*10⁶mm⁴ (6 marks)

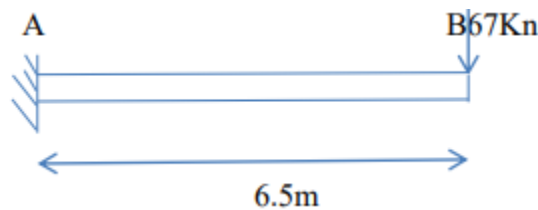


Figure 4

QUESTION TWO (20 MARKS)

Determine the reaction for the continuous beam shown in figure 5 due to the uniformly distributed load and due to the support settlements of 10mm at A , 50mm at B , 20mm at C and 40mm at D. Use the 3 moment equation. E=200GPa and I=700*10⁶mm⁴

$$\begin{aligned} & \frac{M_\ell L_\ell}{I_\ell} + 2M_c \left(\frac{L_\ell}{I_\ell} + \frac{L_r}{I_r} \right) + \frac{M_r L_r}{I_r} \\ &= -\sum \frac{P_\ell L_\ell^2 k_\ell}{I_\ell} (1 - k_\ell^2) - \sum \frac{P_r L_r^2 k_r}{I_r} (1 - k_r^2) - \frac{w_\ell L_\ell^3}{4I_\ell} - \frac{w_r L_r^3}{4I_r} \\ & - 6E \left(\frac{\Delta_\ell - \Delta_c}{L_\ell} + \frac{\Delta_r - \Delta_c}{L_r} \right) \end{aligned}$$

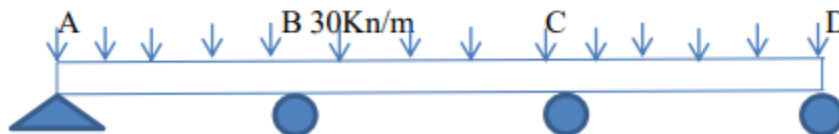


Figure 5

QUESTION THREE (20 MARKS)

A beam ABC of length 9 m has one support at the left end and the other support at a distance of 6m from the left end. The beam carries a point load of 12kN at right end and also 4kN/m over a length of 3m as shown in figure 6. Determine the slope and deflection at point C.

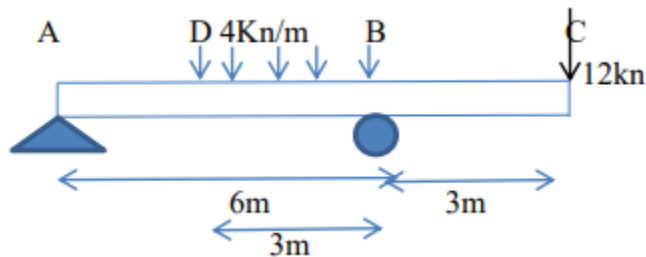


Figure 6

QUESTION FOUR (20 MARKS)

A parabolic arch hinged at the springing and crown has a span of 20m. The central rise of the arch is 4m. It is loaded with a uniformly distributed load of intensity 2kN/m on the left 8m length. Calculate

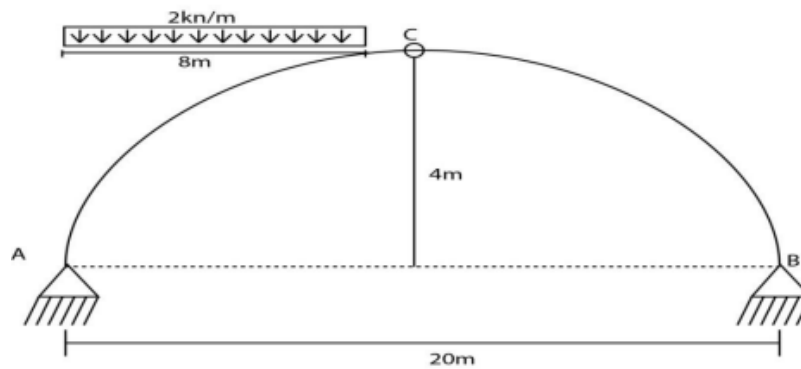


Figure 7

- The direction and magnitude of reactions at the hinges
- The bending moments, normal thrust and shear at 4m and 15m from the left end.
- The maximum positive and negative bending moments

QUESTION FIVE (20 MARKS)

Draw the influence lines for the vertical reactions at support A, C and E, the shear just to the right of C and the bending moment at point B of the beam in figure 7.

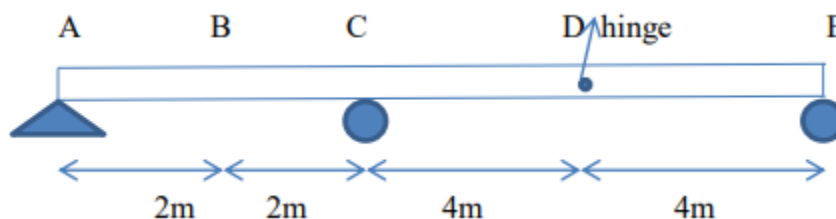


Figure 7