



MACHAKOS UNIVERSITY

University Examinations 2019/2020

SCHOOL OF PURE AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

FIRST YEAR SECOND SEMESTER EXAMINATION FOR

DIPLOMA IN ELECTRICAL ENGINEERING (TVET)

2601/103/M: MATHEMATICS

DATE: 24/3/2020

TIME: 11.30-2.30 PM

INSTRUCTIONS:

The paper consists of EIGHT questions. Answer any FIVE questions.

ALL questions carry equal marks.

Show all your working

QUESTION ONE

a) Simplify the expressions

i)
$$\frac{(1-x)^{\frac{1}{2}} - x(1-x)^{\frac{-1}{2}}}{1-x}$$

ii)
$$\frac{\log 729 - \frac{1}{3}\log 81 + 2\log 27}{\log 243 - \frac{1}{3}\log 27 + \log 9}$$
 (7 marks)

b) Solve the equations

i. $\log_3(2x-3) = -1$

ii. $3^{2x} = 4(3^x) + 3$

iii. $4^x = 2 + 16^{\frac{x}{4}}$ (13 marks)

QUESTION TWO

Solve

a) $5x - 3y - 2z = 31$

$$2x + 6y + 3z = 4$$

$$4x + 2y - z = 30$$
 (8 marks)

b) $2\log_a(x+1) + \log_3 x = 1$ (6 marks)

c) $3\cosh x - 7\sinh x = 2$ correct to 3 decimal places (6 marks)

QUESTION THREE

- a) i $\frac{1-\cos\theta}{\sin\theta} + \frac{\sin\theta}{1-\cos\theta} = 2\operatorname{cosec}\theta$
- ii $\tan 3x = \frac{3\tan x - \tan^3 x}{1-3\tan^2 x}$ (8 marks)
- b) i $\cosh 2x = \frac{1+\tanh^2 x}{1-\tanh^2 x}$
- ii $\tanh 3x = \frac{3\tanh x + \tanh^3 x}{1+3\tanh^2 x}$ (6 marks)
- c) $\cos x + \cos(x+120^\circ) + \cos(x+240^\circ) = 0$ (6 marks)

QUESTION FOUR

- a) Given $Z = \frac{1}{2+j^3} + \frac{1}{1-j^2}$, express Z in the form $a+bj$ (5 marks)
- b) Express $Z = (2-7j)$ in polar form (4 marks)
- c) Given the complex numbers $z_1 = 2+5j$, $z_2 = 1-3j$ and $z_3 = 2+3j$ determine $4z_1^2 + 3z_2z_3$. (7 marks)
- d) Express $\frac{2+3j}{3+4j}$ in the form $a + bj$ (4 marks)

QUESTION FIVE

- a) Solve the following equation for all values of θ between 0° and 360°
 $2\sin \theta - 3\cos \theta = 2$ (6 marks)
- b) Solve for x given $3^{2x} = 4(3^x) + 3$ (4 marks)
- c) Show that $\frac{1+\tan^2 B}{1+\cot^2 B} = \tan^2 B$ (6 marks)
- d) Given that $(a+b) + j(a-b) = 9 + 10j$, find the values of a and b . (4 marks)

QUESTION SIX

- a) Given that $\sin A = \frac{4}{5}$ and $\cos B = \frac{5}{13}$ where A is obtuse and B is acute, determine the values of
- i. $\cos (A+B)$
- ii. $\tan (A+B)$ (7 marks)
- b) Given that $p\cosh x + q\sinh x = 3e^x - 2e^{-x}$, determine the values of p and q . (7 marks)
- c) Solve the equation $\frac{jx}{1+jy} = \frac{3x+jy}{x+3y}$ (6 marks)

QUESTION SEVEN

- a) Express in polar co-ordinates the position :
- $P_1(3, 4)$
 - $P_2(-5, -8)$ (6 marks)
- b) Obtain the Cartesian equations of;
- $r = 5(1 + 2\cos\theta)$
 - $r = a \tan\theta$ (7 marks)
- c) Find the cartesian equations of the loci;
- $x = t^2 + 4$ and $y = t - 3$
 - $x = 5\cos\theta$ and $y = 4\sin\theta$ (7 marks)

QUESTION EIGHT

- a) Given the complex numbers $Z_1 = 4 + 3j$, $Z_2 = 1 + j$ and $Z_3 = 1 - 2j$, express $Z = Z_1 + \frac{Z_2 Z_3}{Z_2 + Z_3}$ in the form $a + bj$. (8 marks)
- b) Use De Moivre's theorem to prove that $\cos 3\theta = 4\cos^3\theta - 3\cos\theta$ (5 marks)
- c) Given that $Z = j$ is one root of the equation $Z^4 - 2Z^3 + 3Z^2 - 2Z + 2 = 0$, determine the other roots. (7 marks)